



# Evaluation of the Jason-1 ground retracking algorithm

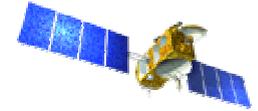
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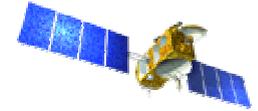


# Objective

The objective of this presentation is to give an overview of some of the results that have been obtained with the Jason-1 retracking algorithms and especially with the retracking algorithm used for the GDR 'B'.

Additional results have already been provided during the OSTST in Arles and in St.Petersburg and also in the 2<sup>nd</sup> and 3<sup>rd</sup> Marine Geodesy special issues on Jason-1.

## Historical reminder of the Jason-1 retracking algorithm



- Since launch, GDRs have been obtained with a retracking algorithm (MLE-3)
  - ✓ solving for 3 parameters (SWH, epoch and amplitude)
  - ✓ using a Hayne's model developed at the first order (valid for  $\xi < 0.3\text{deg}$ )
  - ✓ with a skewness coefficient of 0
  - ✓ corrected with LUT (coherent with the rtk algorithm)

**→ GDR 'A'**
  
- Star tracker system has shown abnormal behavior leading to mispointing angles out of the limit of validity of the model
  
- Development of a second order model valid up to 0.8 deg  
(Amarouche, 2004, Marine Geodesy 2nd issue)
  
- Impossibility to derive the mispointing angle from the slope of the trailing edge
  
- Development of a new retracking algorithm (MLE-4)
  - ✓ solving for 4 parameters (SWH, epoch, amplitude + mispointing angle)
  - ✓ using the model developed at the second order (valid for  $\xi < 0.8\text{deg}$ )
  - ✓ with a skewness coefficient of 0.1
  - ✓ corrected with LUT (coherent with the new rtk algorithm)

**→ GDR 'B'**

# Analytical formulation of the waveform model



- 1st order model ( for mispointing angles lower than  $0.3^\circ$  )  
(Hayne's model)

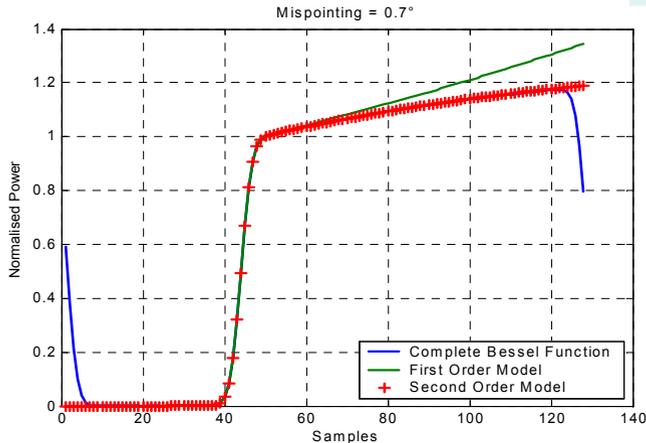
$$W(t) = A \exp(-v) [1 + \operatorname{erf}(u)]$$

With :

$$u = \frac{t - \tau - \alpha \sigma_c^2}{\sqrt{2} \sigma_c} \quad v = \alpha \left( t - \tau - \frac{\alpha}{2} \sigma_c^2 \right) \quad \alpha = \delta \frac{\beta^2}{4}$$

- 2nd order model ( for mispointing angles lower than  $0.7^\circ$  ) (Amarouche, 2004, Marine Geodesy 2nd issue)

$$W(t) = A \exp(-v_1) [1 + \operatorname{erf}(u_1)] - \frac{A}{2} \exp(-v_2) [1 + \operatorname{erf}(u_2)]$$



With :

$$u_1 = \frac{t - \tau - \alpha_1 \sigma_c^2}{\sqrt{2} \sigma_c} \quad v_1 = \alpha_1 \left( t - \tau - \frac{\alpha_1}{2} \sigma_c^2 \right) \quad \alpha_1 = \delta \frac{\beta^2}{8}$$

$$u_2 = \frac{t - \tau - \alpha_2 \sigma_c^2}{\sqrt{2} \sigma_c} \quad v_2 = \alpha_2 \left( t - \tau - \frac{\alpha_2}{2} \sigma_c^2 \right) \quad \alpha_2 = \delta$$

$$\delta = \frac{4c}{\gamma h} \cos(2\xi) \quad \beta = 4 \left[ \frac{c}{h} \right]^{1/2} \sin(2\xi)$$

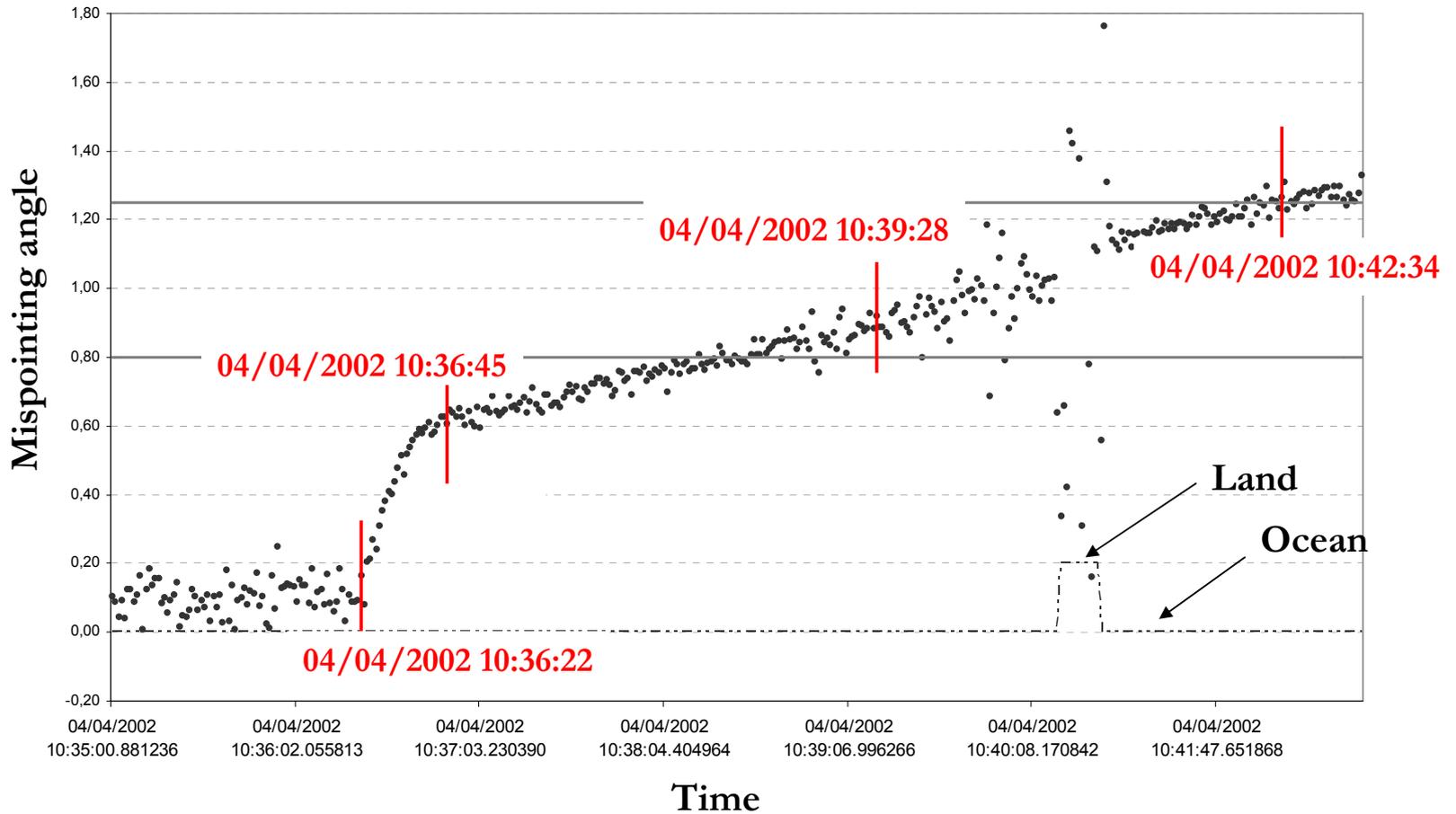
- Consequences on the retracking procedure

impossibility to derive the mispointing angle from the slope of the trailing edge

~~$$\xi^2 = \frac{1}{2} \frac{1 + \frac{\text{Slope}}{\alpha}}{1 + \frac{\alpha}{\gamma}}$$~~

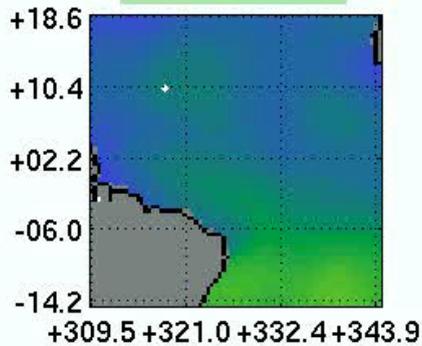
➔ MLE retracking solving for 4 parameters (range, SWH,  $\sigma_0$  and  $\xi^2$ )

# First Star Tracker Incident (Cycle 008 : 04/04/2002)

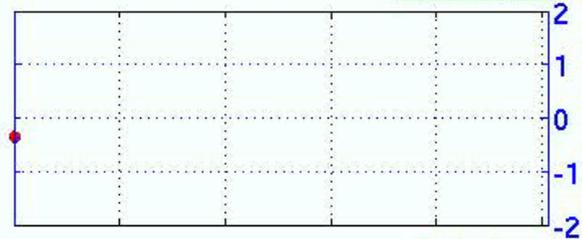


Jason-1 : Cycle 008 / Pass 252 / 10H35m8s => 10H40m13s

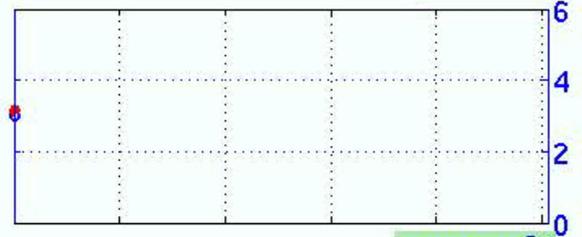
Satellite Track



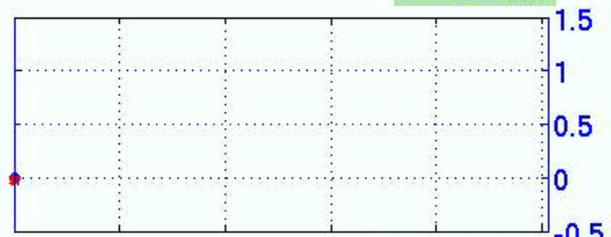
Epoch [m]



SWH [m]



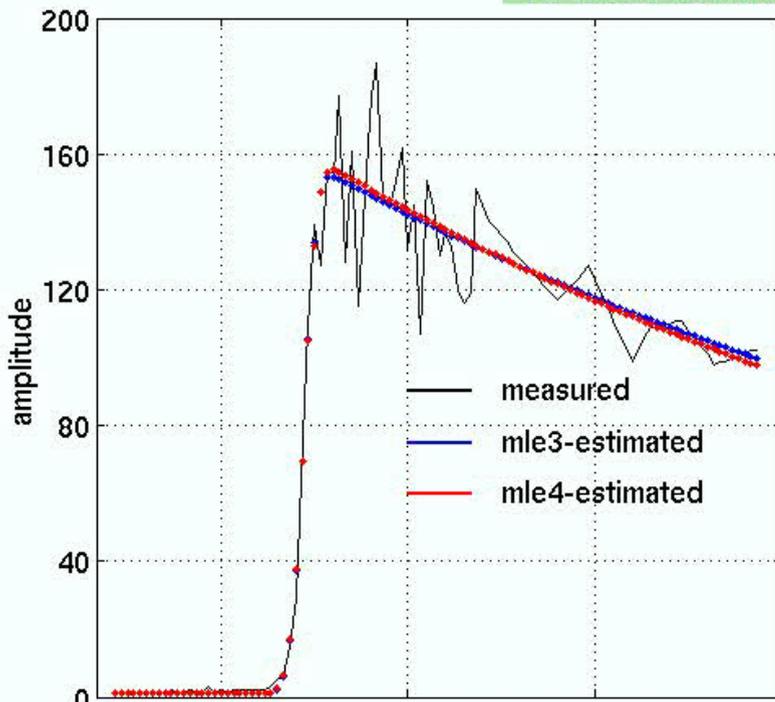
$\chi^2$  [deg<sup>2</sup>]



$\sigma_0$  [dB]

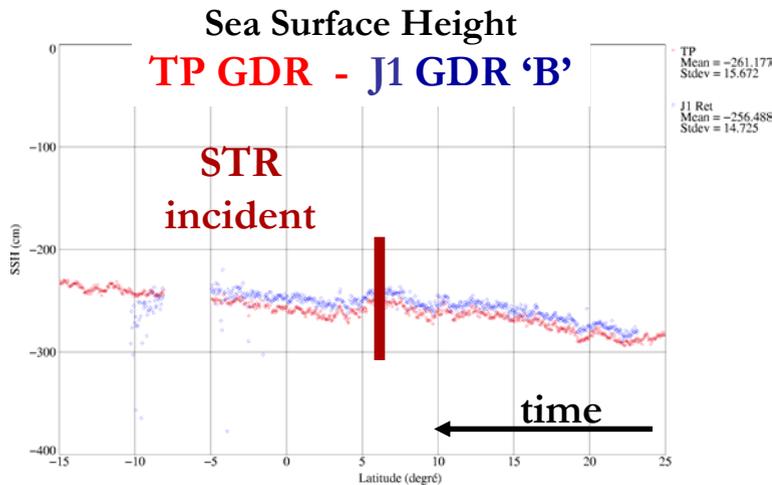
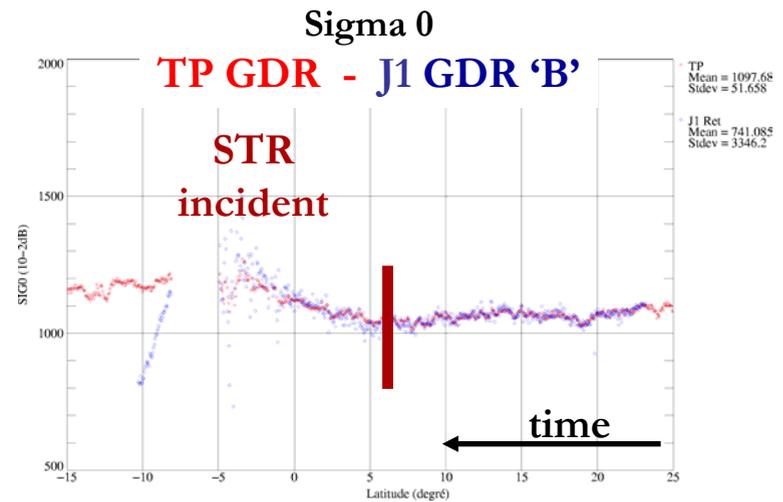
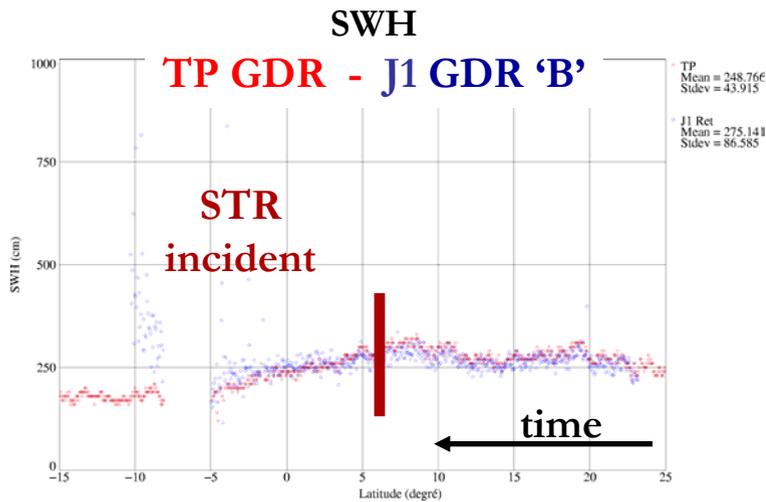
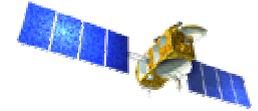


Ku-Band Waveforms



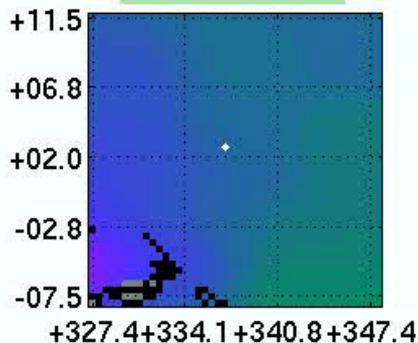
seconds

# Comparison with Topex data (separated by 73 sec) on 04/04/2002

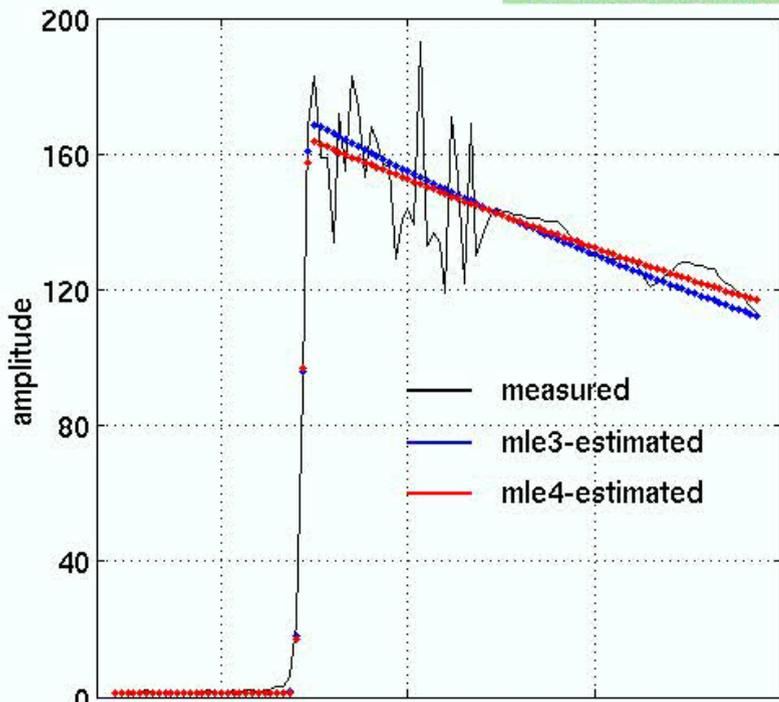


Jason-1 : Cycle 128 / Pass 162 / 19H21m33s

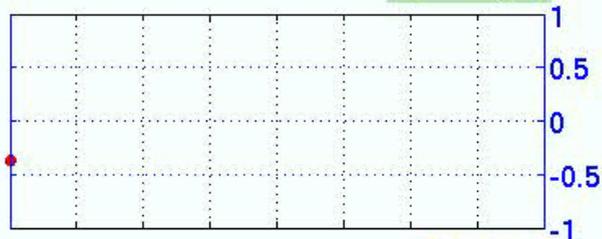
Satellite Track



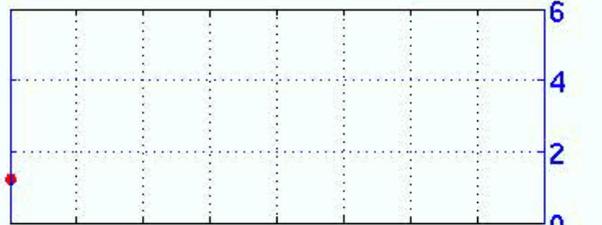
Ku-Band Waveforms



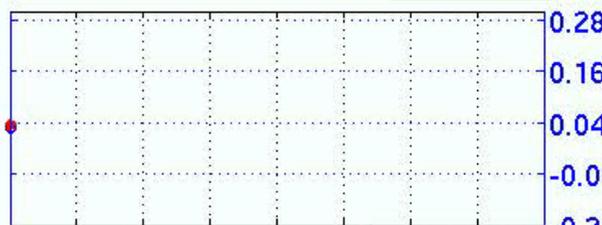
Epoch [m]



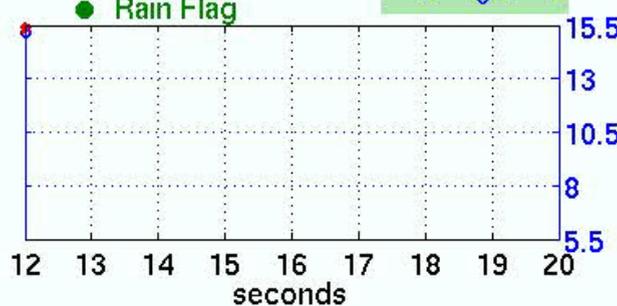
SWH [m]



$\Xi_2$  [deg<sup>2</sup>]



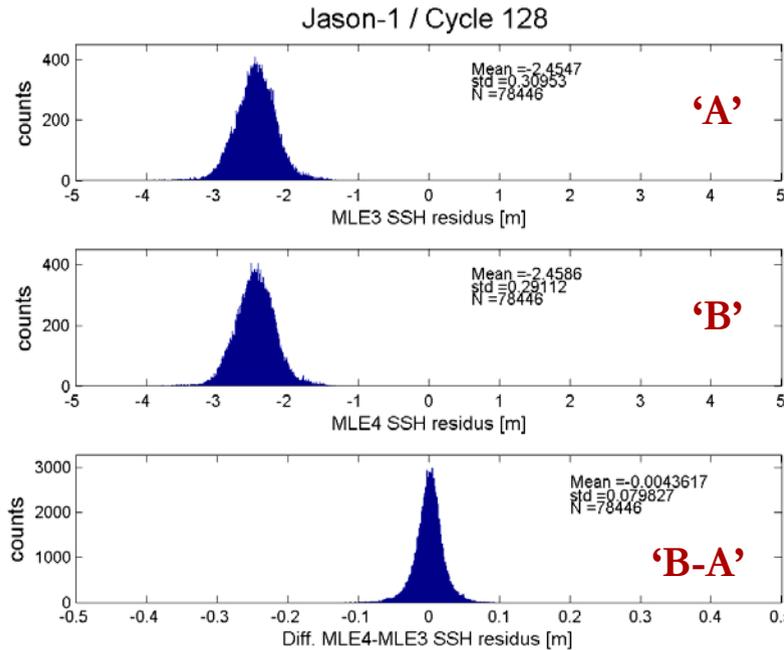
$\sigma_0$  [dB]



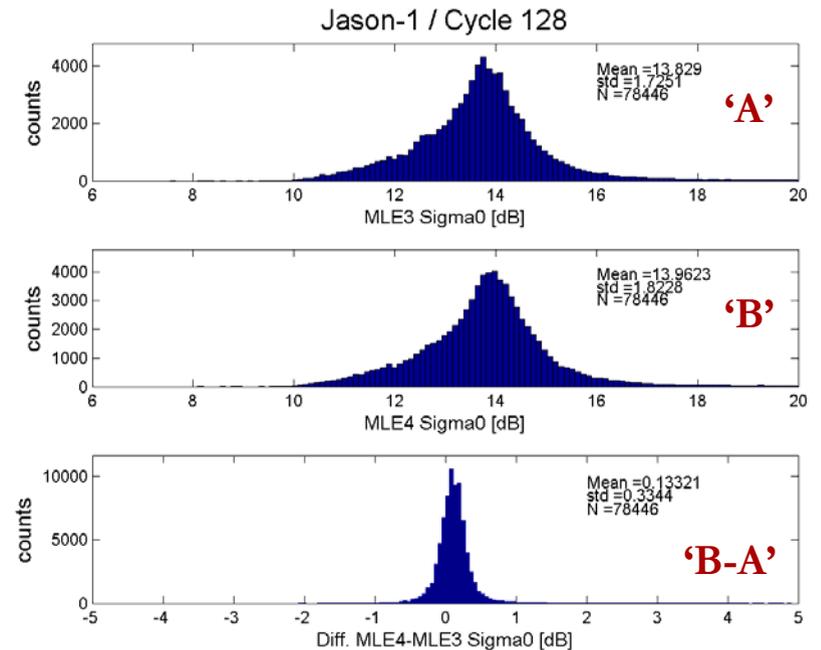


# Histograms of the main parameters (Cycle 128)

## Res SSH



## Sigma0

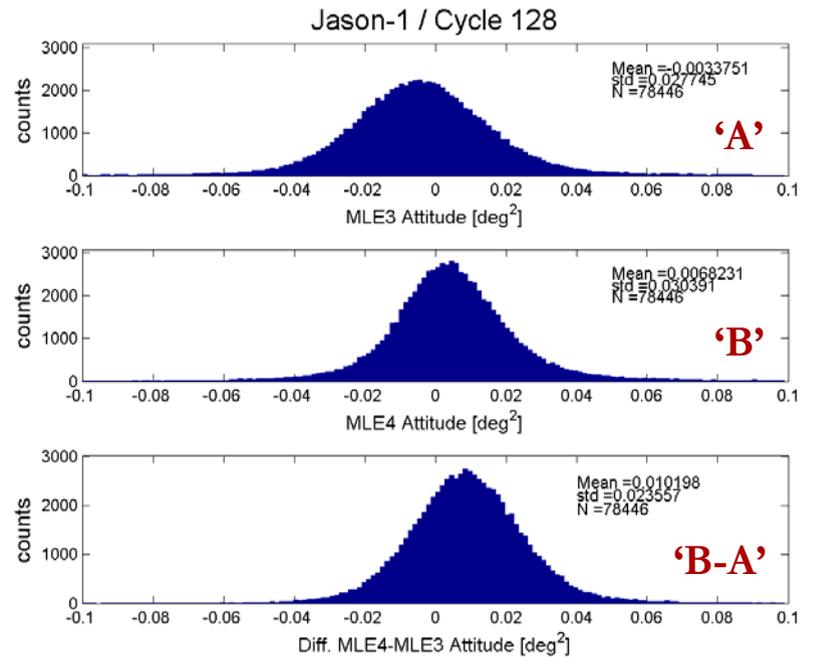
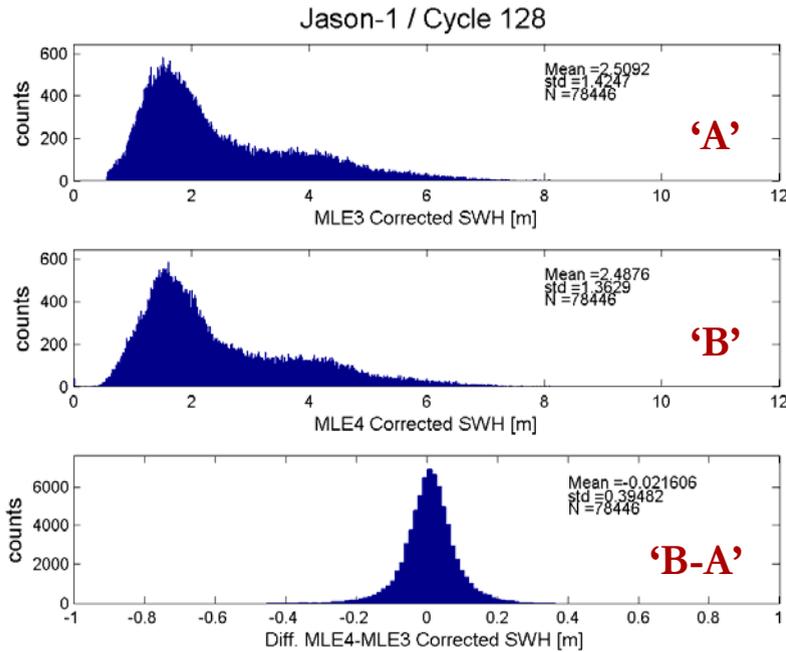




# Histograms of the main parameters (Cycle 128)

## SWH

## $\xi^2$



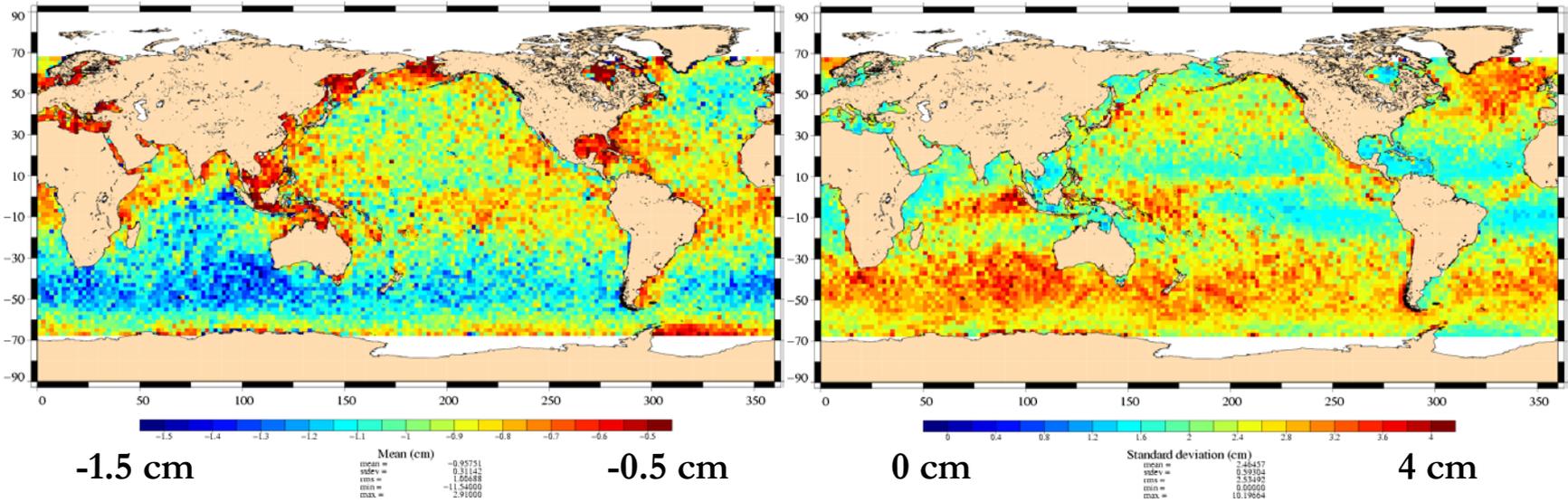


## Difference of range without LUT : GDR 'B' – GDR 'A'

Mean

Cycles 1-21

Std



➔ Impact of the Retracking algorithm (weak on mean, significant on Std )

➔ Impact of the skewness coefficient (0.3%SWH)

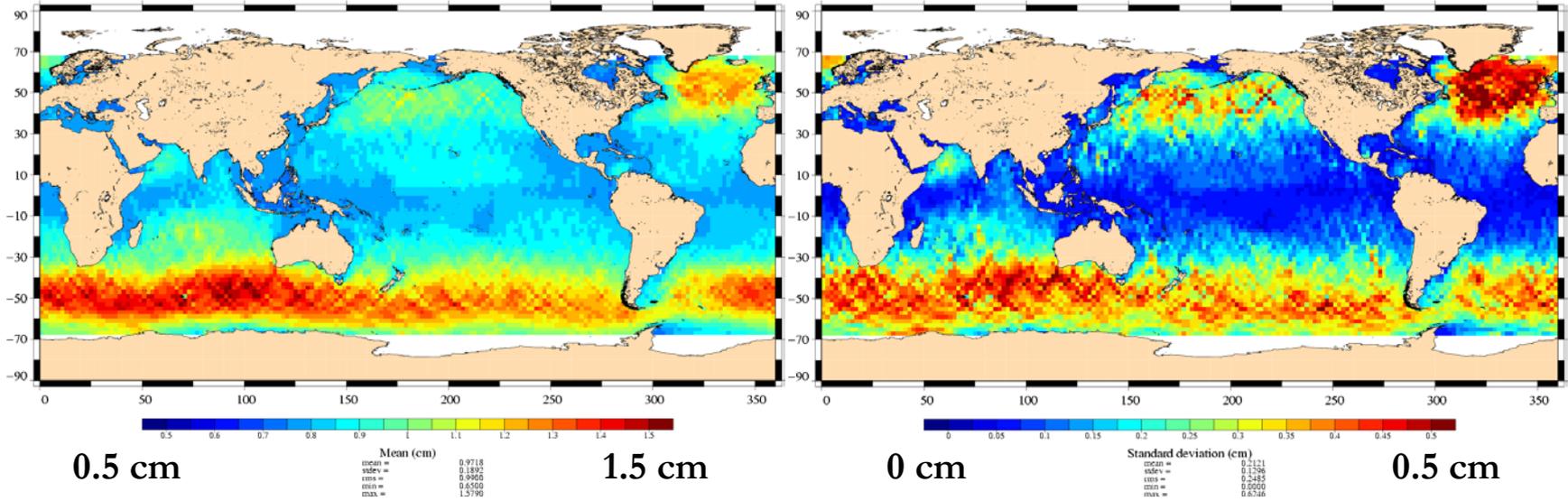


# Differences of LUT on range : GDR 'B' – GDR 'A'

Mean

Cycles 1-21

Std



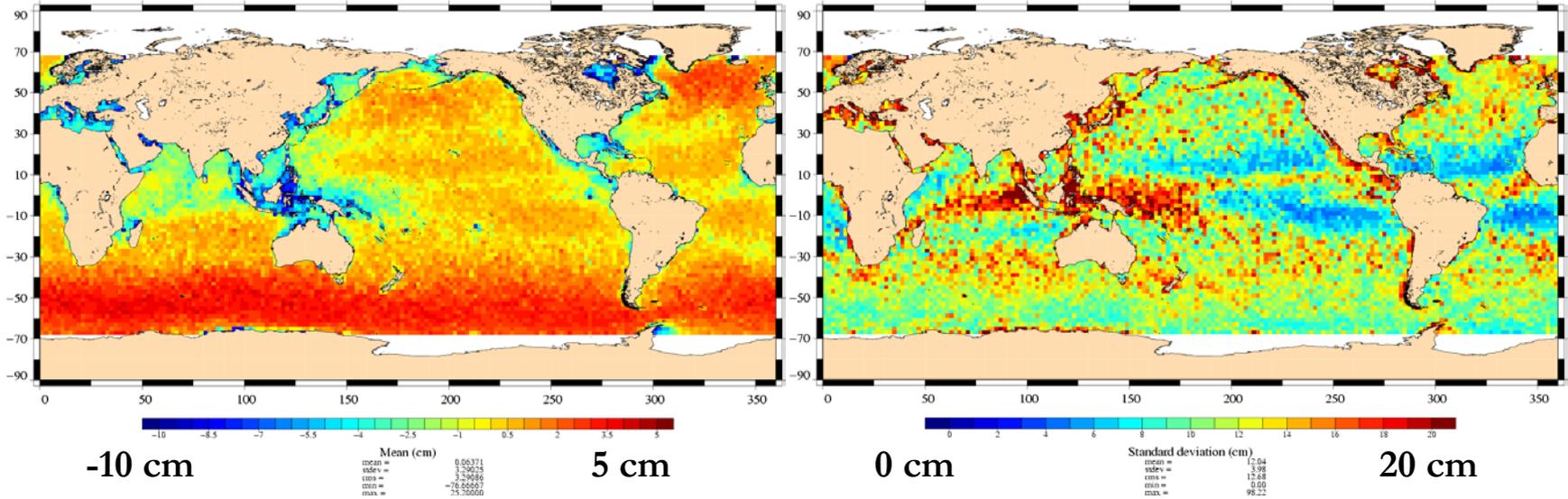


# Difference of Significant Wave Height : GDR 'B' – GDR 'A'

Mean

Cycles 1-21

Std



➔ Impact of the LUT : higher values of SWH for GDR 'B' than for GDR 'A'

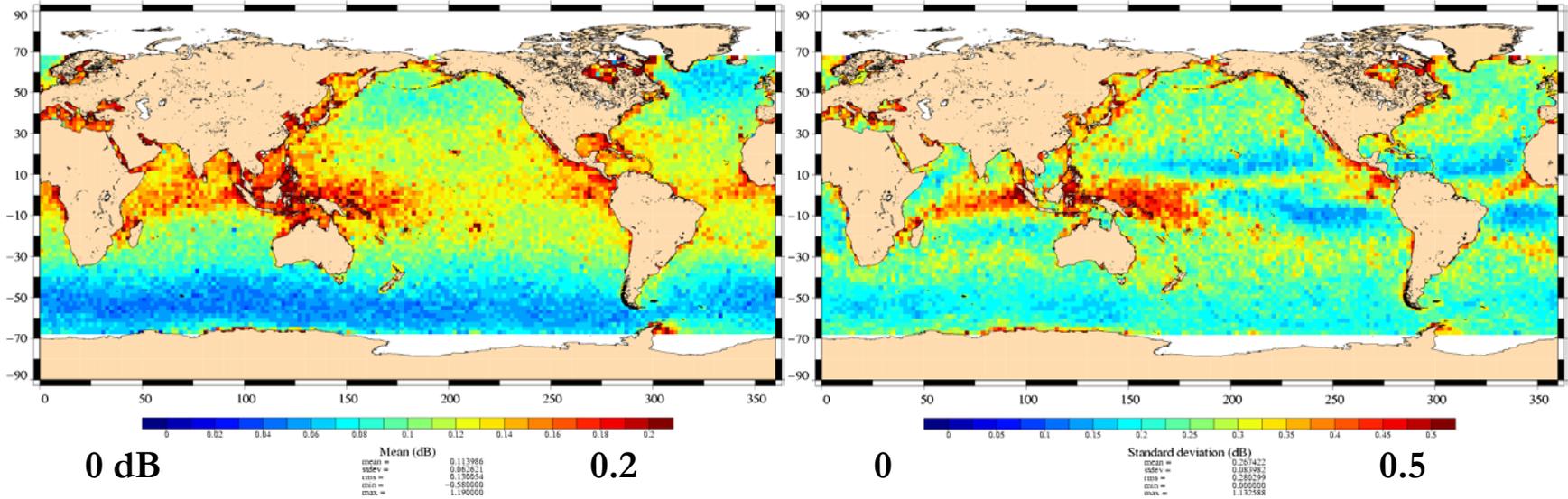


## Difference of Sigma naught : GDR 'B' – GDR 'A'

Mean

Cycles 1-21

Std



- ➔ Mean bias equal to 0.1 dB
- ➔ No impact of the LUT
- ➔ Very small impact of the retracking

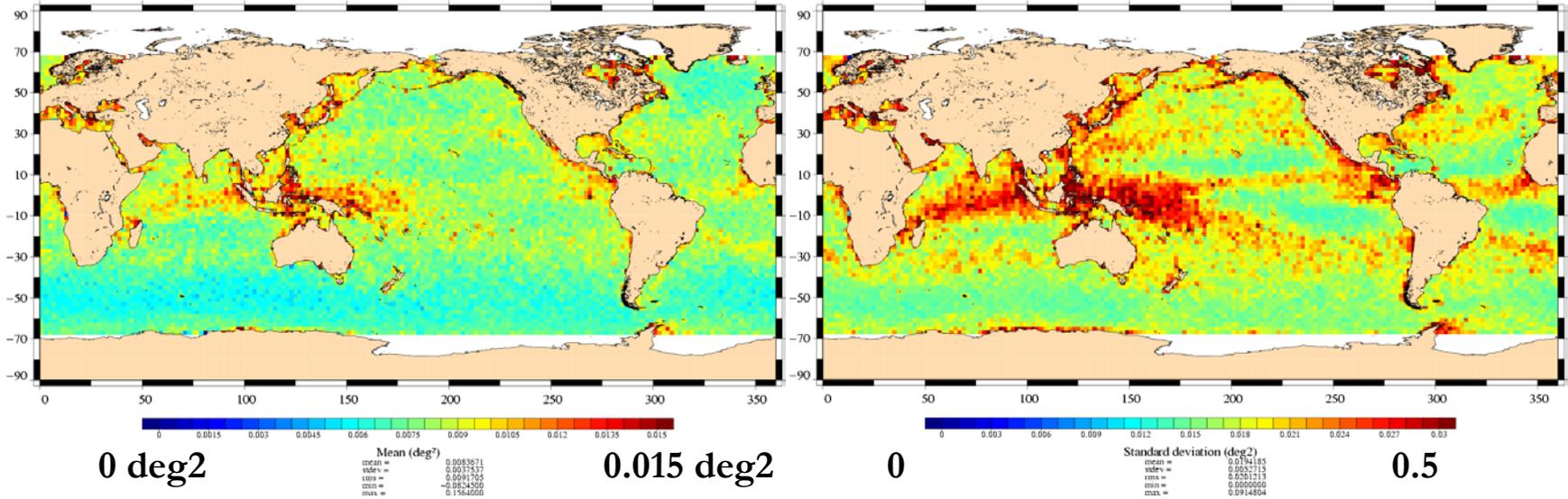


# Difference of ATT square : GDR 'B' - GDR 'A'

Mean

Cycles 1-21

Std



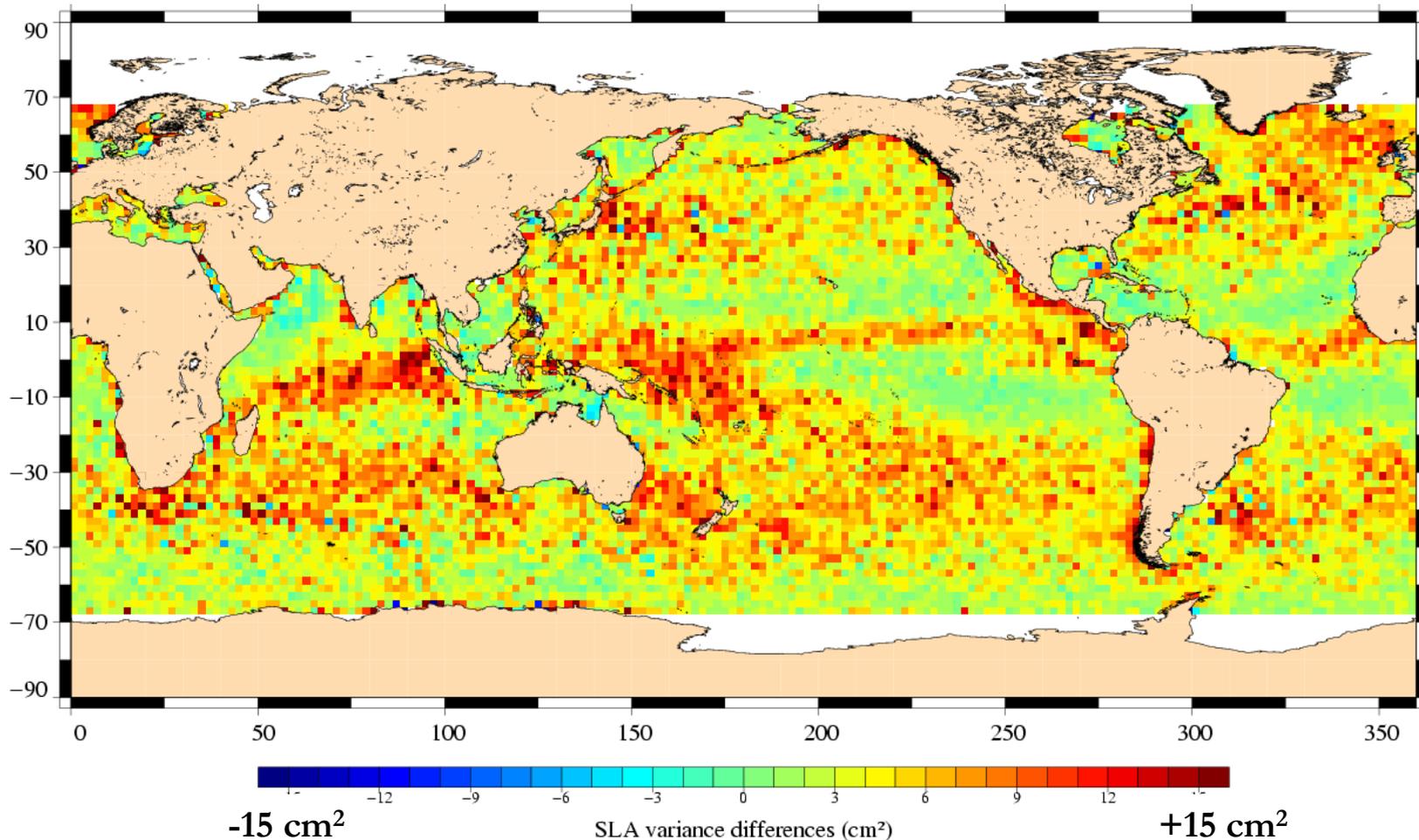
➔ Bias on the mean value (from negative to slightly positive)

# Variance reduction (between GDR 'B' and GDR 'A')

→ Always positive



## SLA variance differences

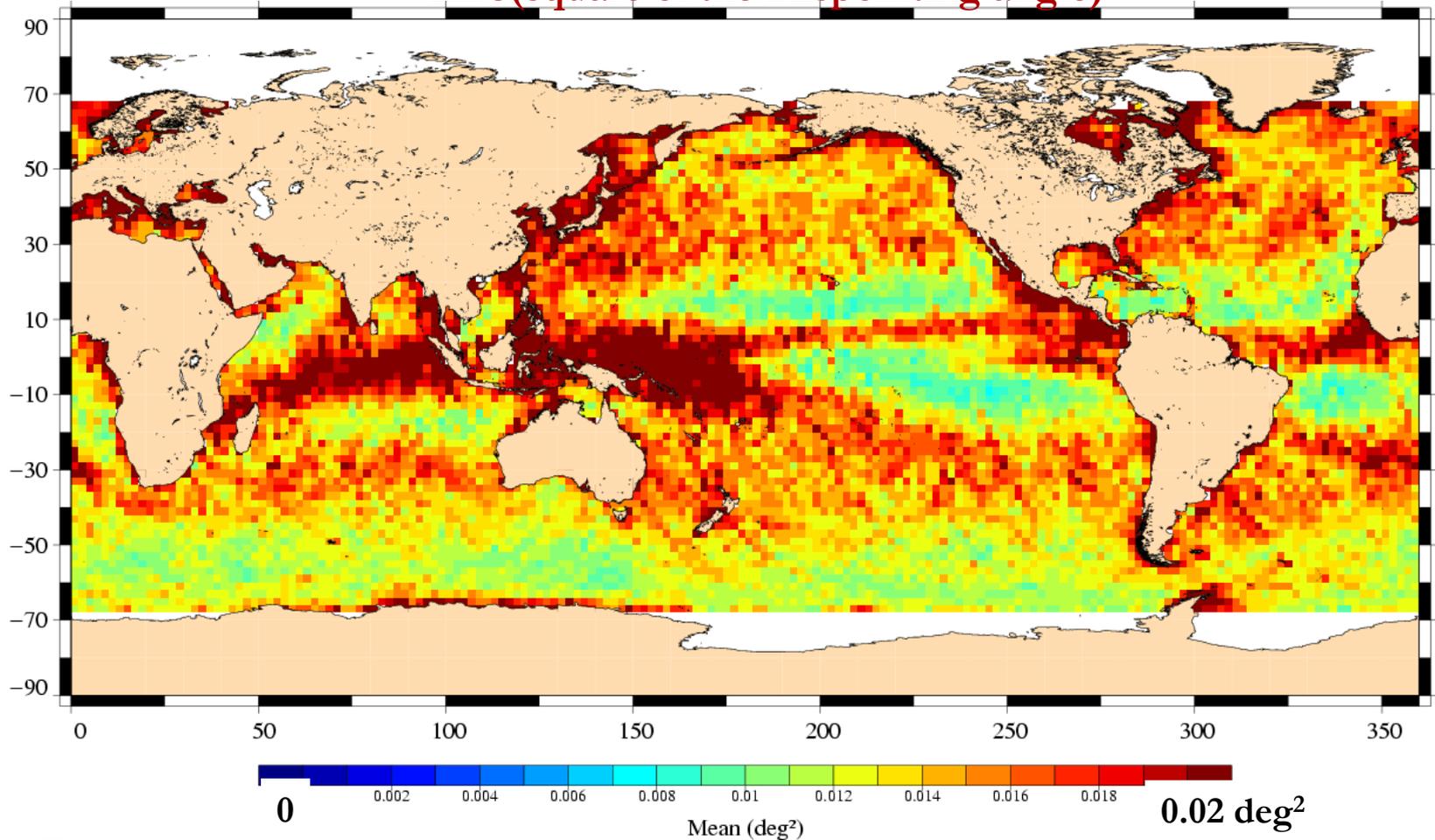


→ Every where the waveforms differ from the theoretical Hayne's model (especially in the trailing edge of the WF), the MLE-4 retracking algorithm performs better than MLE-3 with reduction of the variance of the SLA.



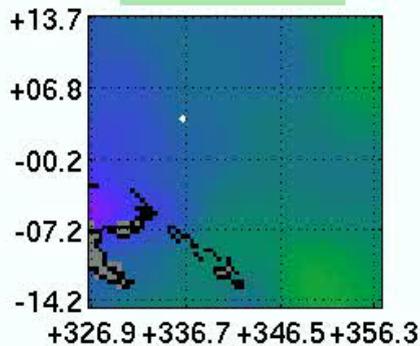
→ Pseudo mispointing angle different from real mispointing angle

**ABS(square of the mispointing angle)**



Jason-1 : Cycle 128 / Pass 162 / 19H20m53s

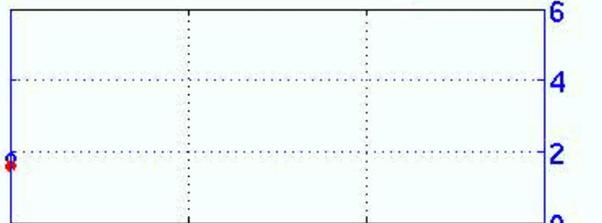
Satellite Track



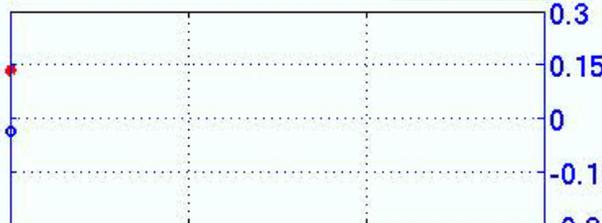
Epoch [m]



SWH [m]

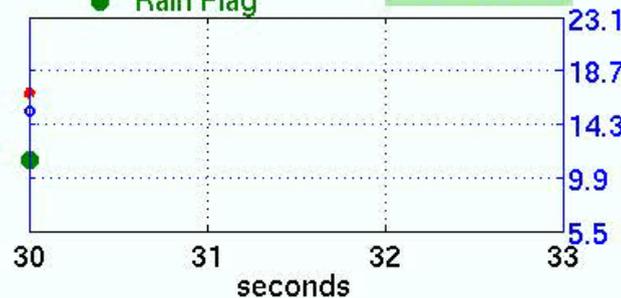


$\chi^2$  [deg<sup>2</sup>]

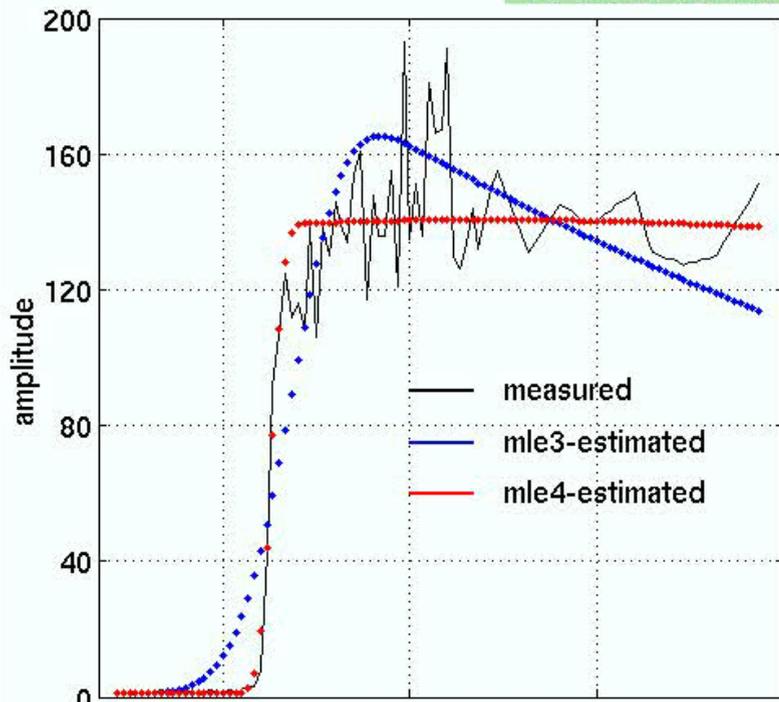


$\sigma_0$  [dB]

● Rain Flag



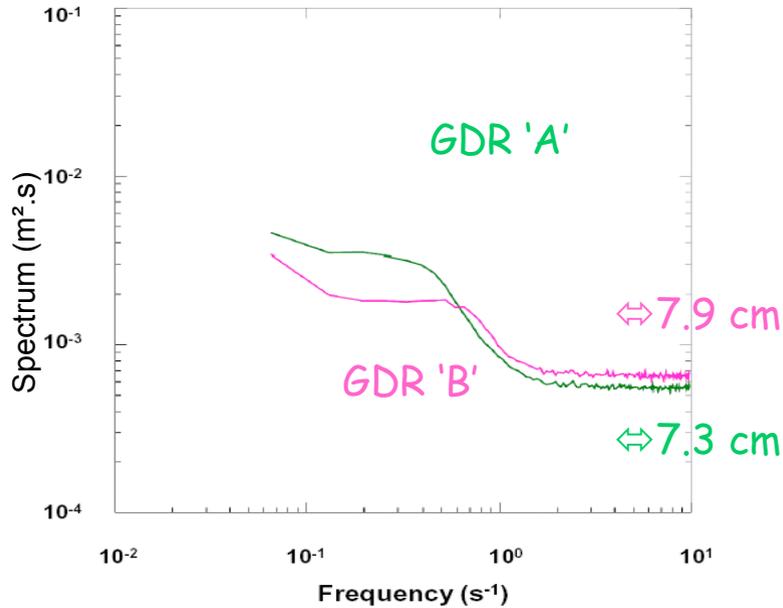
Ku-Band Waveforms



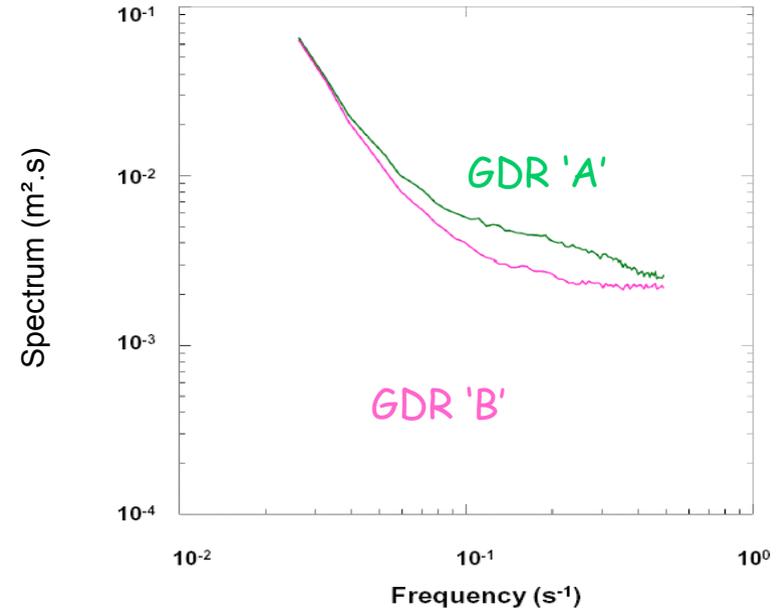


## Jason-1 SSH spectra (cycle 131)

### 20 Hz



### 1 Hz

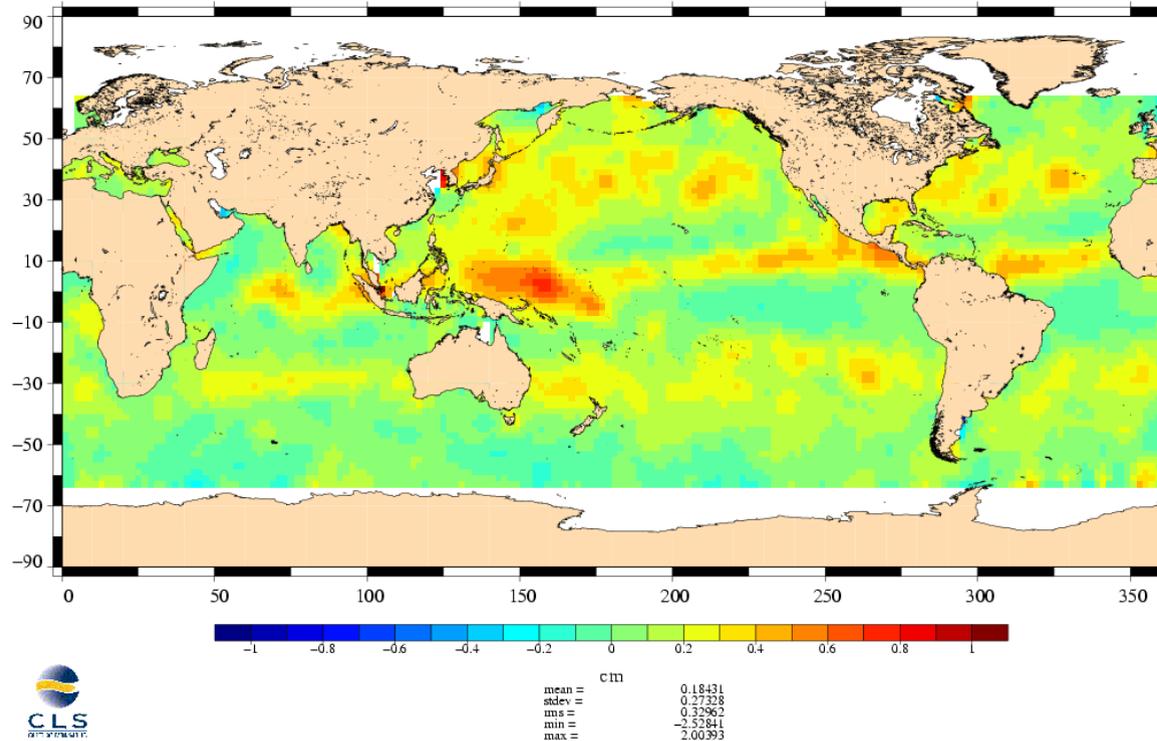


- ➔ Increase of the 20-Hz noise level
- ➔ Drop in energy in the range [0.1Hz-1Hz]

- ➔ Drop in energy in the range [0.1Hz-1Hz]

Comparison with Envisat data are developed by Y.Faugère (CalVal and Data consistency session)

# Jason-1 high frequency reduction : GDR 'A' – GDR 'B' - cycles 128 - 135



→ Areas where the high frequency content is decreased : rain areas

See again comparison with Envisat by Y.Faugère (CalVal and Data consistency session)



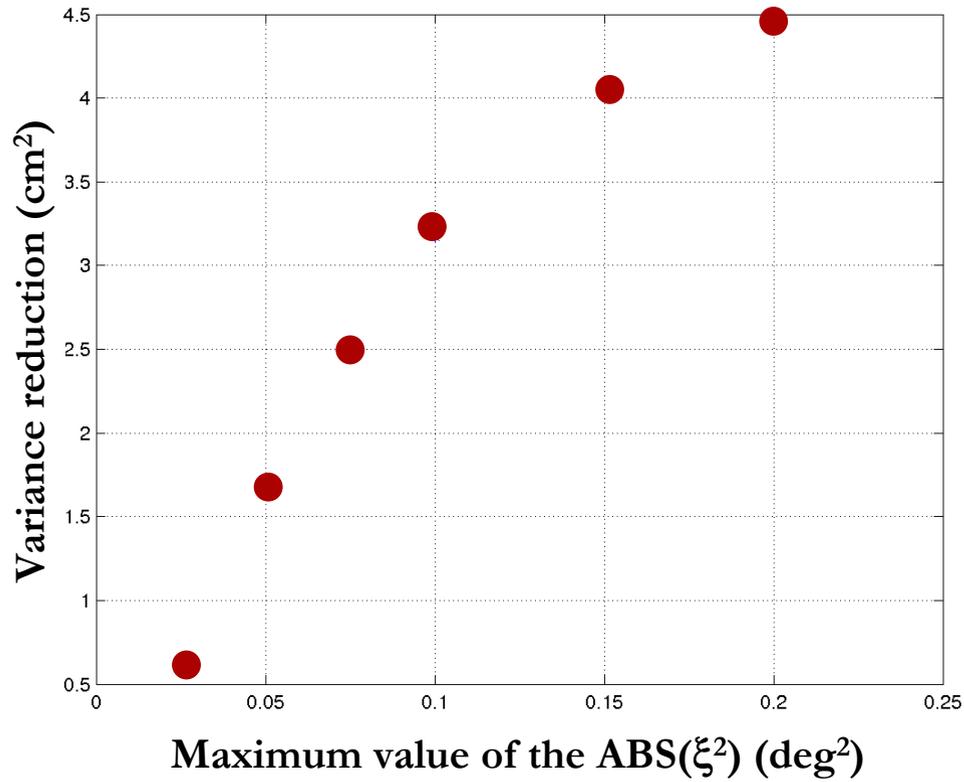
# CONCLUSION

GDR 'B' using MLE-4 with second order model fully validated :

- On platform sequences with real mispointing (up to 0.8 deg)
  - On “normal Hayne’s echoes” with a slight increase of the 20Hz noise but a drop of the spectrum energy in the range [0.1Hz-1Hz]
  - On corrupted echoes (rain, sigma blooms, ...) (variance reduction)
- ➔ Envisat retracking algorithm ? What results could be expected ?



# Variance difference 'B'- 'A' as a function of the max value of the mispointing



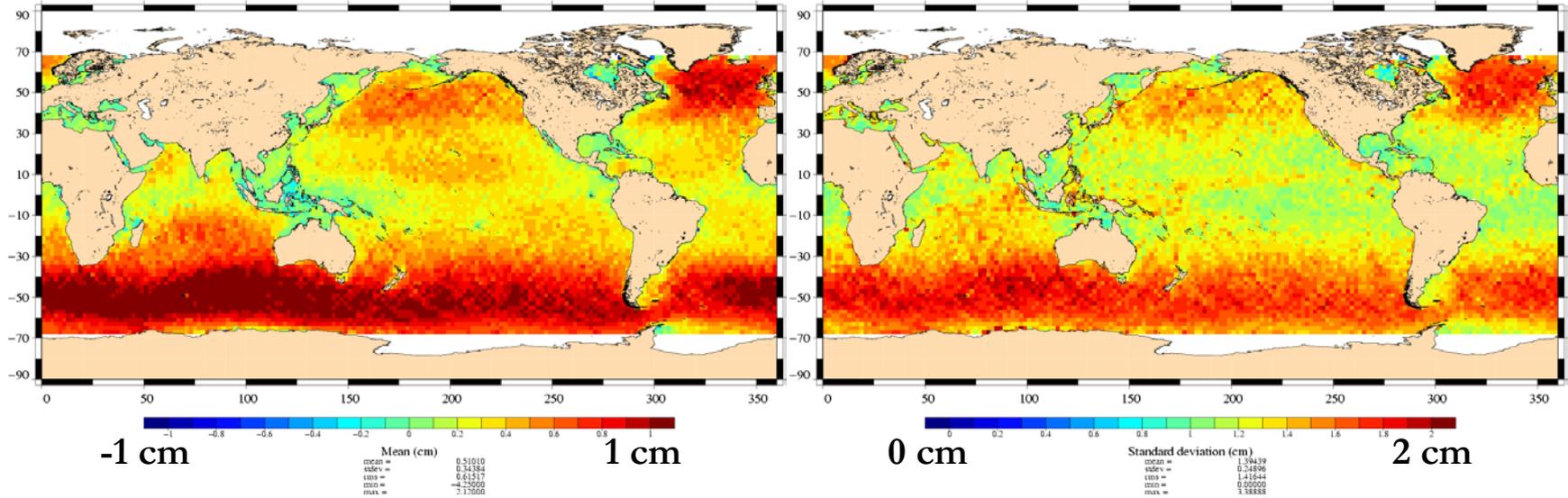
# Difference of standard deviation on range (20 Hz data) : 'B' - 'A'



Mean

Cycles 1-21

Std



➔ Correlation with SWH (high waves)

# Jason-1 SSH spectrum (cycle 131)



20 Hz

Low  $\xi^2 \rightarrow \xi^2 < 0.025 \text{ deg}^2$

