

An Investigation into the Source of the 59-Day Variations in Jason Sea Level

*E. W. Leuliette¹, R. Scharroo^{1,2}, W. H. F. Smith¹,
J. L. Lillibridge¹, and L. Miller¹*

¹NOAA/Laboratory for Satellite Altimetry

²Altimetrics LLC

Special thanks to Gary Mitchum





Questions to be addressed



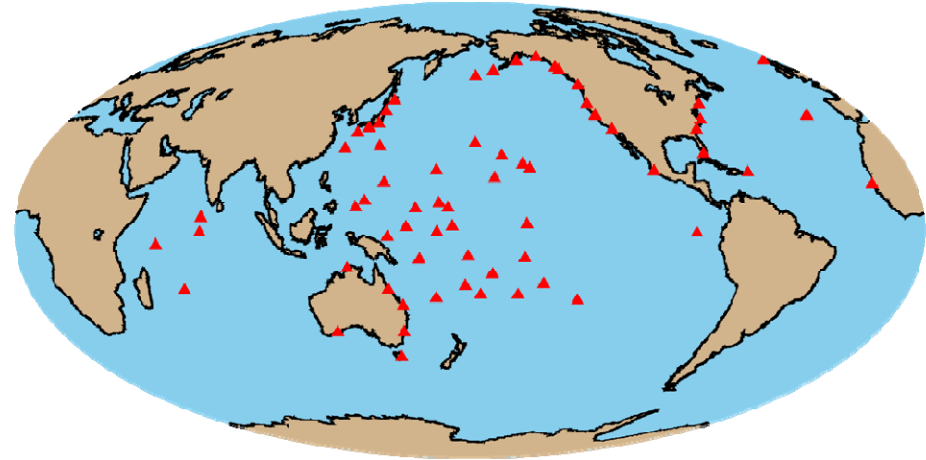
Is the TOPEX CoG correction valid?

How do J1–TX orbit – range differences depend on sun angle and orbital parameters?

Can an empirical correction based on J1–TX cal phase differences remove the 59-day & semi-annual in the J1 time series?

Mitchum tide gauge calibration without S2 alias removed

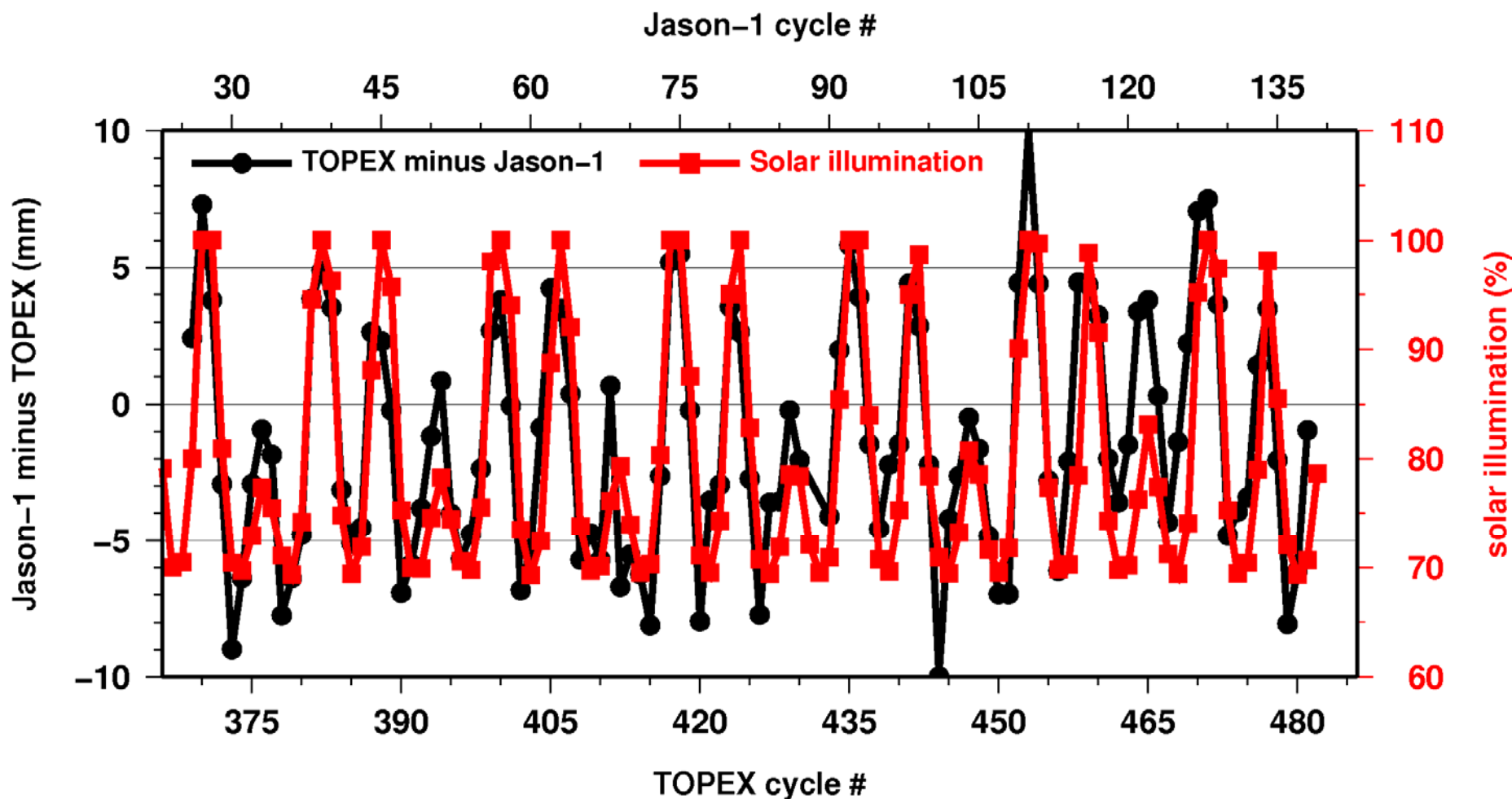
- No IB correction for TX or gauges
- No tide model applied to gauges, GOT4.7 applied to TOPEX



Amplitude (mm) and phase of 58.77 day signal

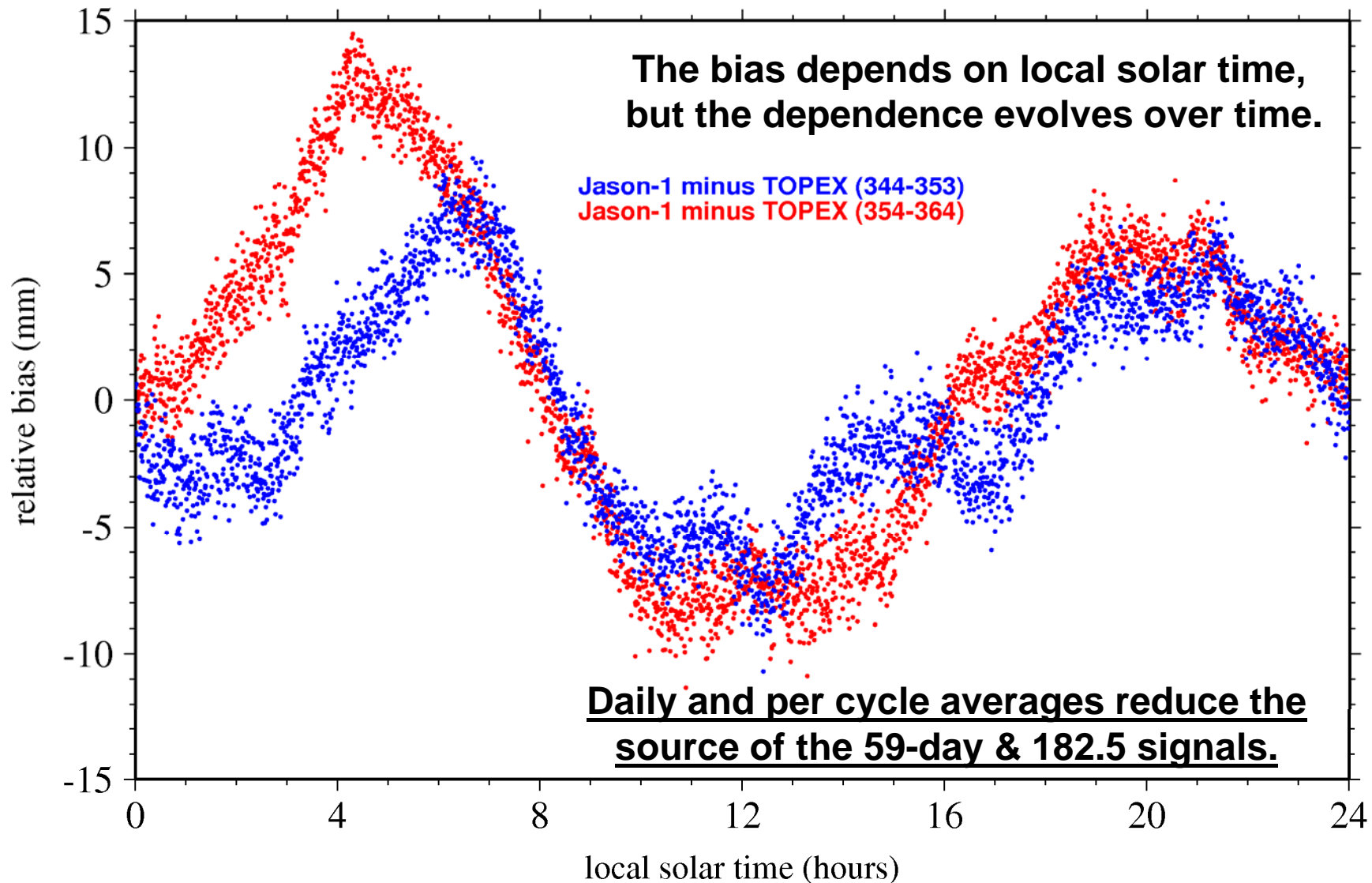
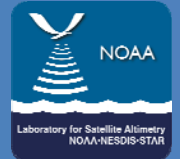
cycles	1 – 364	1 – 235	236 – 364
Weighted gauges	2.4 (205°)	1.6 (200°)	3.2 (197°)
TOPEX@gauges (CoG applied)	2.5 (193°)	2.3 (183°)	2.3 (191°)
TOPEX@gauges (no CoG)	3.2 (196°)	4.8 (197°)	4.4 (192°)
TOPEX (CoG) – gauges	0.5 (103°)	0.8 (142°)	0.9 (17°)
TOPEX (no CoG) – gauges	2.3 (188°)	2.8 (185°)	1.6 (205°)

For per-cycle global means, the J1-TX bias is highly corrected with the amount of time TX/J1 spent in the Sun.





J1-TX bias versus solar time



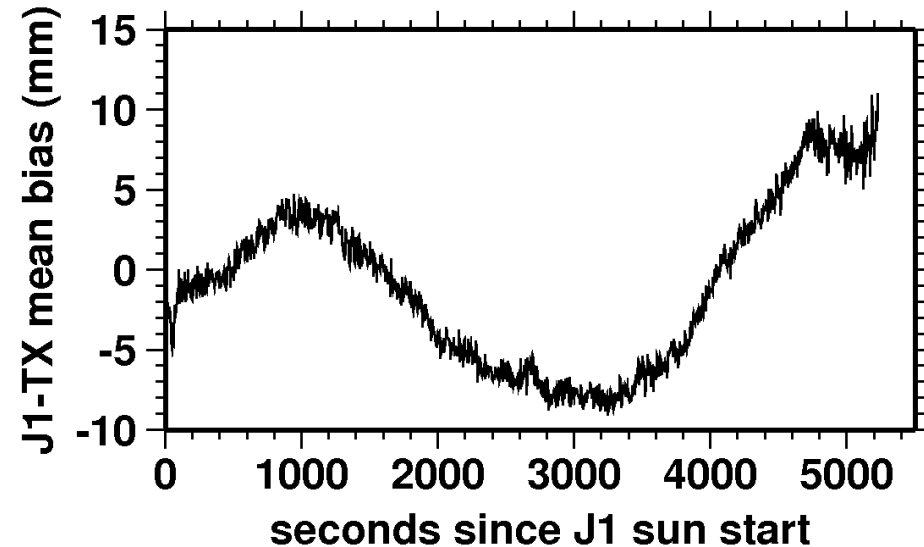


Bias behavior in/out of eclipse



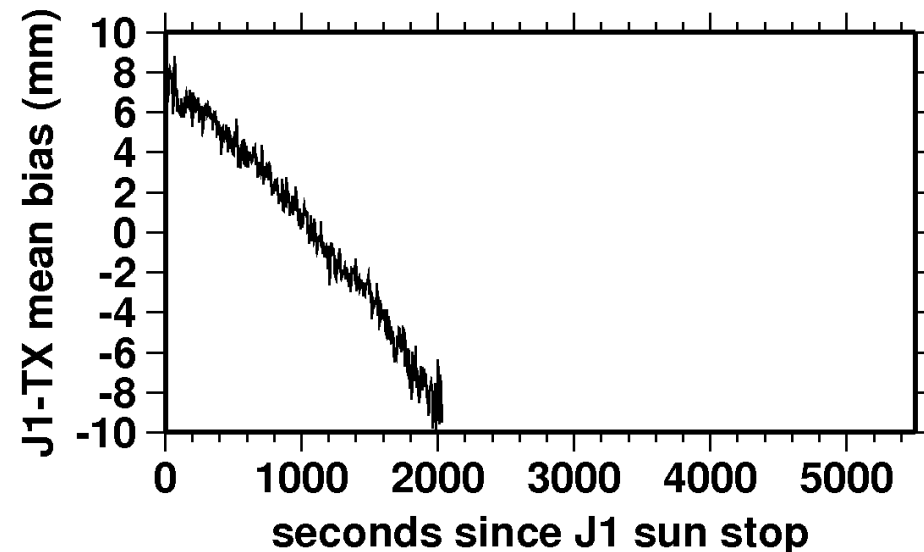
Mean bias after J1-TX leaves eclipse

Not simply a problem at S2 frequency



Mean bias after J1-TX enters eclipse

The 18 mm linear drift in range implies a thermal effect in one of the instruments



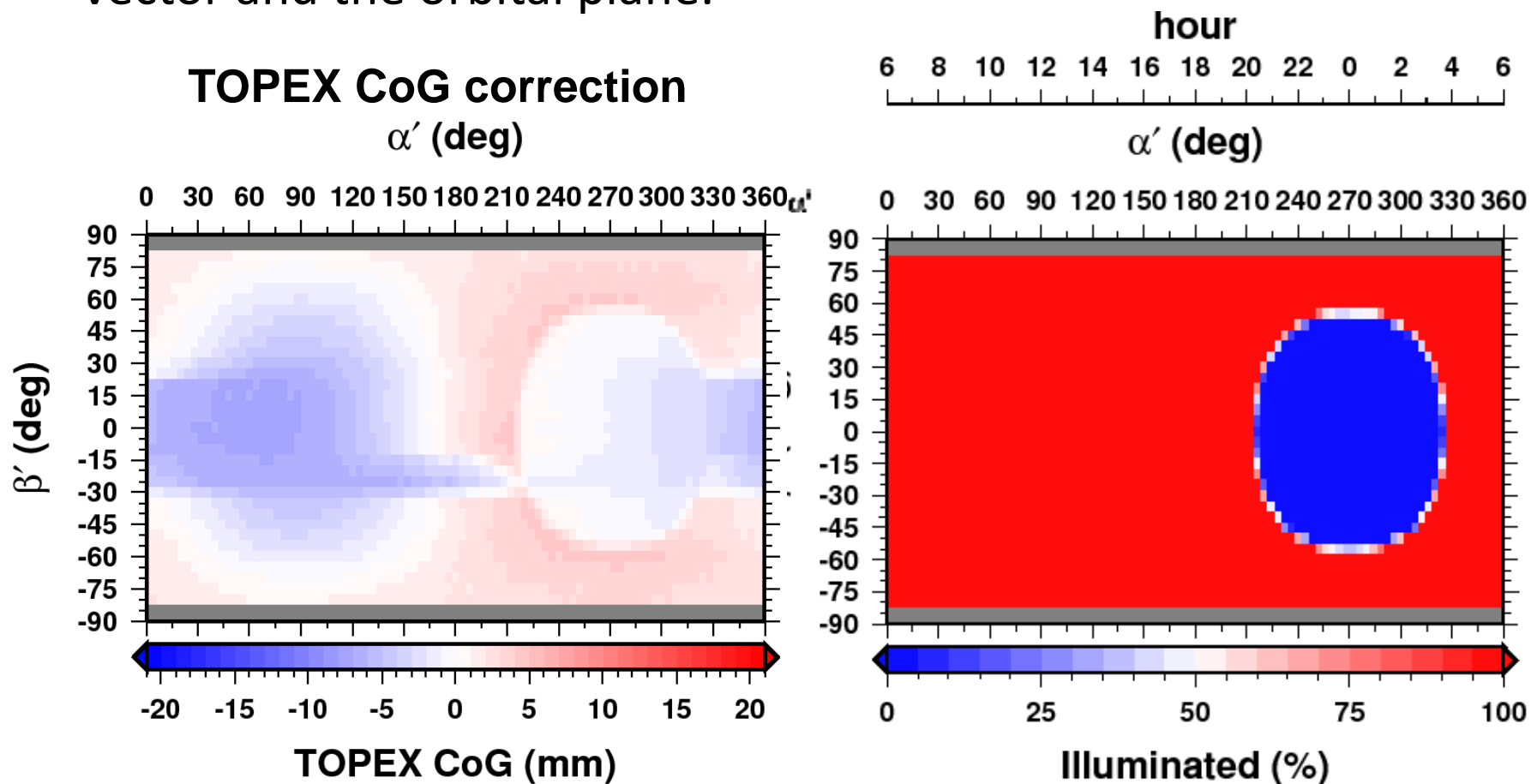


TOPEX Center of Gravity correction



α' , orbit angle, i.e. the angular separation of the spacecraft from the orbital 6 a.m. position.

β' , solar aspect angle, i.e. the angle between the Earth/Sun position vector and the orbital plane.



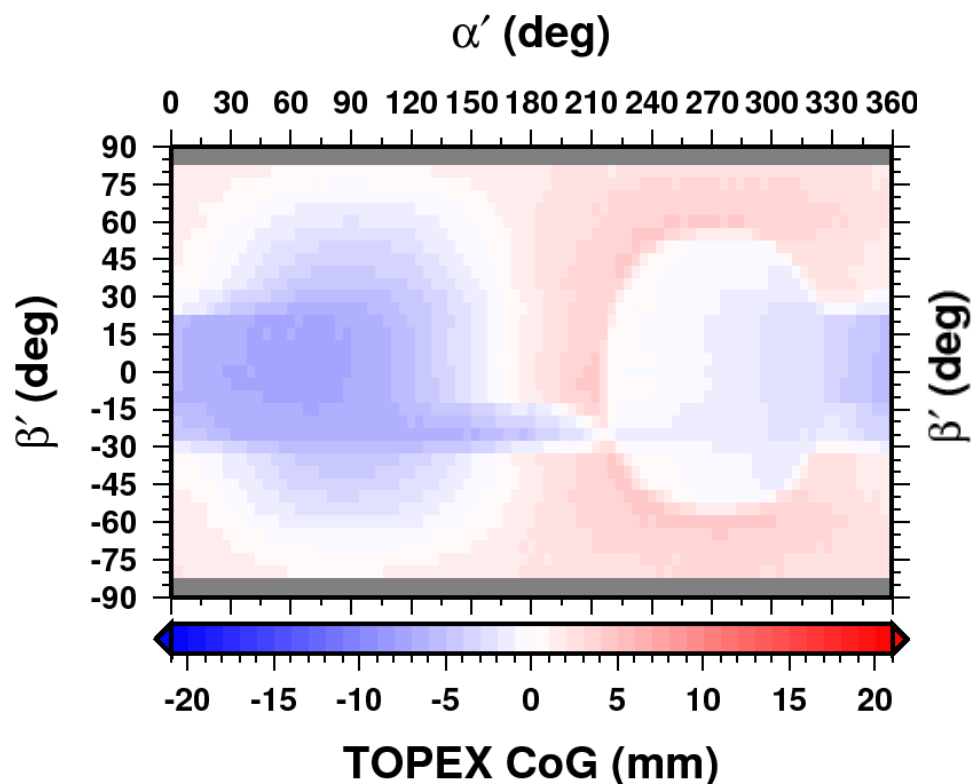


Tide models and TX CoG correction

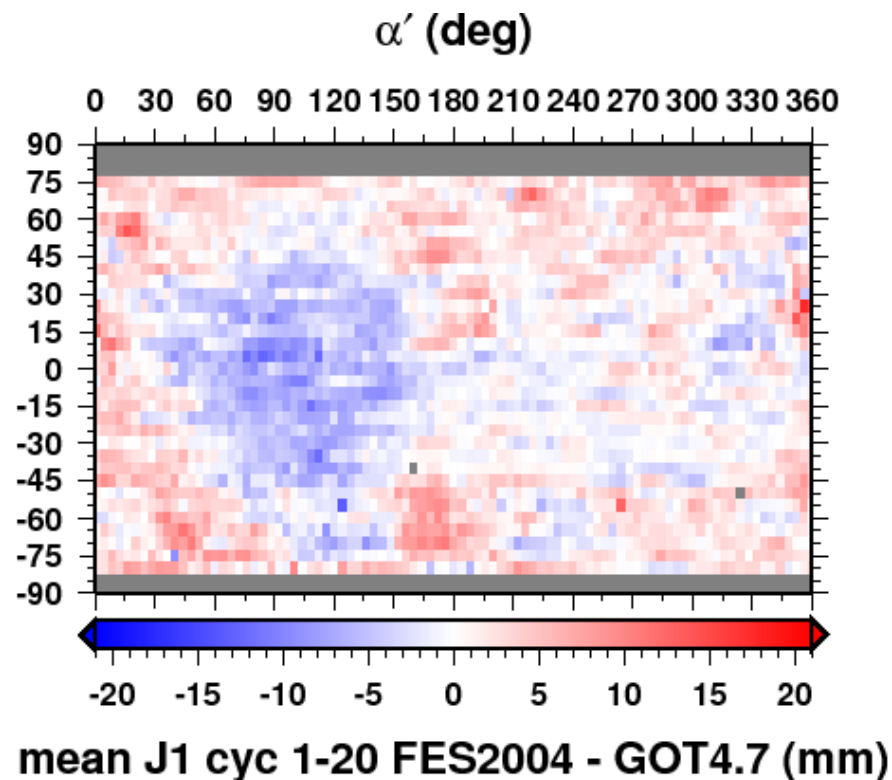


The differences between FES2004 and GOT4.7 is of similar to the TOPEX center of gravity correction.

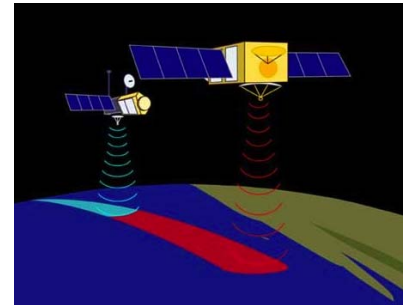
**TOPEX CoG correction
Cycles 344 – 364**



**Difference in FES2004 & GOT4.7
Jason-1 cycles 1–20**

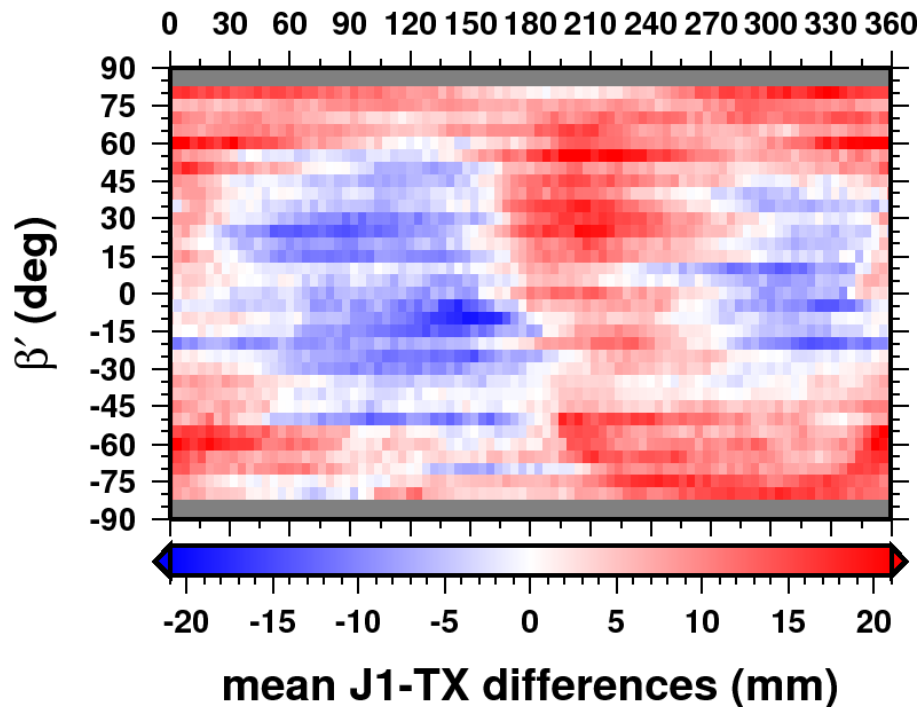


8 727 638 calibration phase differences binned 4° in α' and 5° in β'



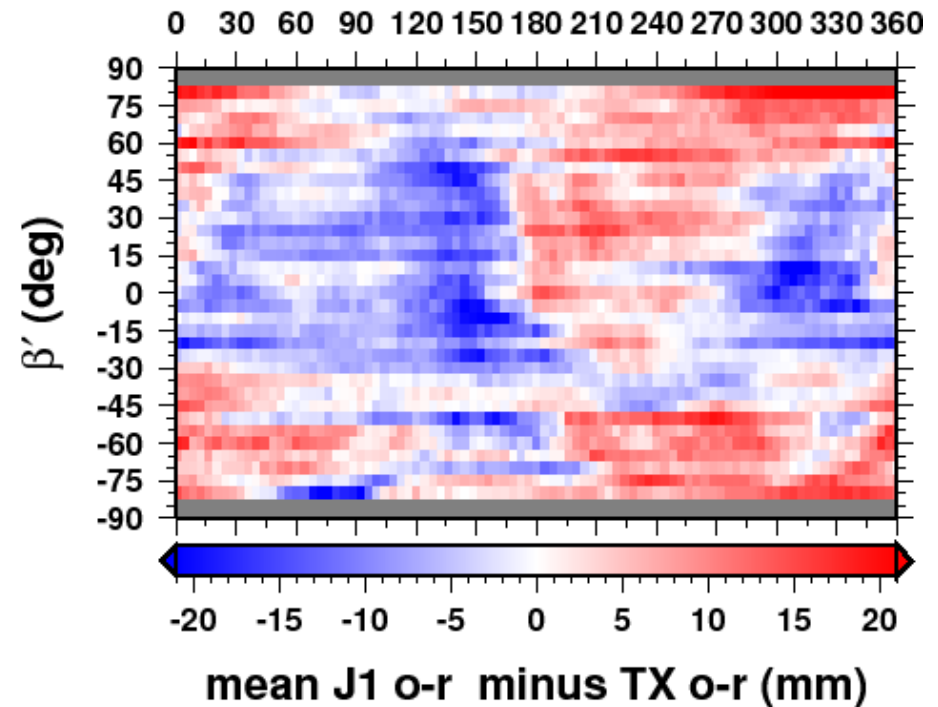
Sea level

α' (deg)



Orbit – range

α' (deg)

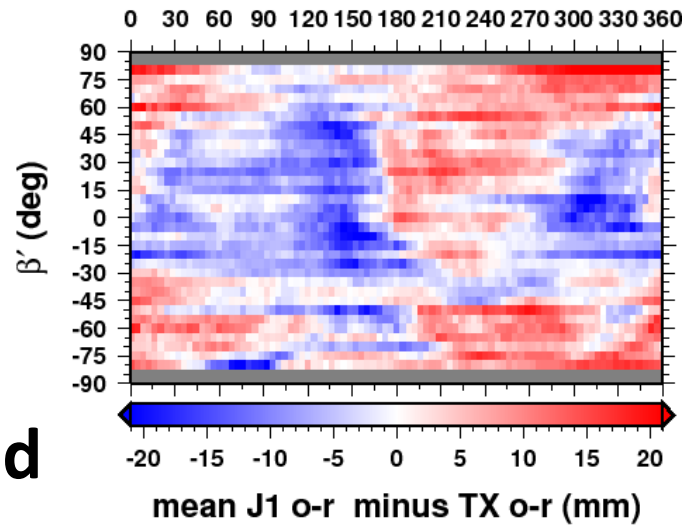




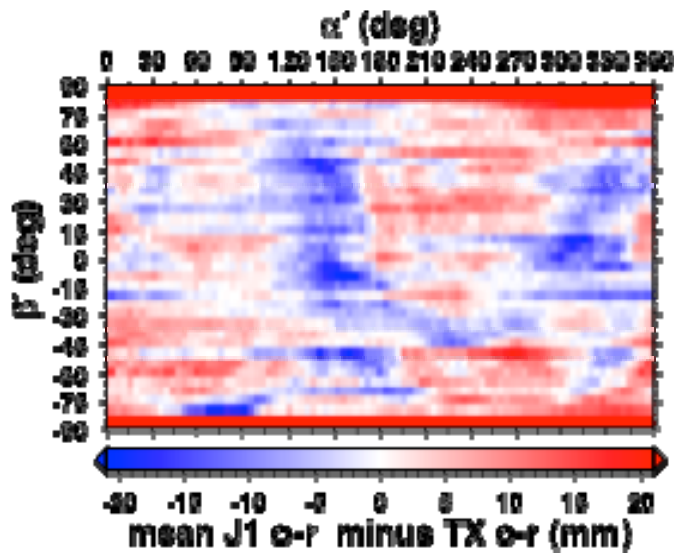
TX CoG applied to orbit-range



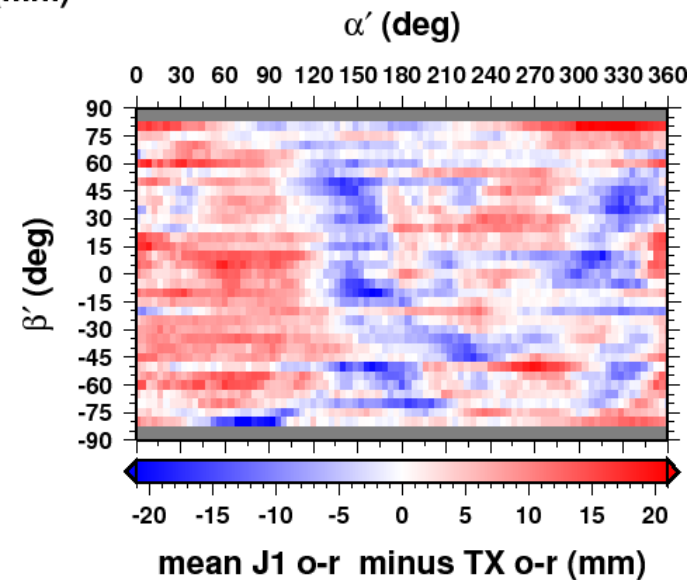
CoG applied (-) α' (deg)



CoG not applied



CoG sign flip (+)





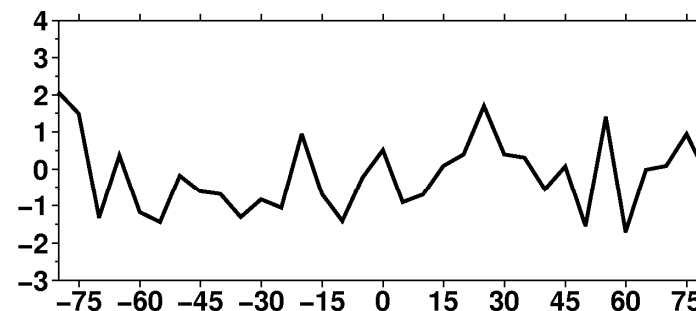
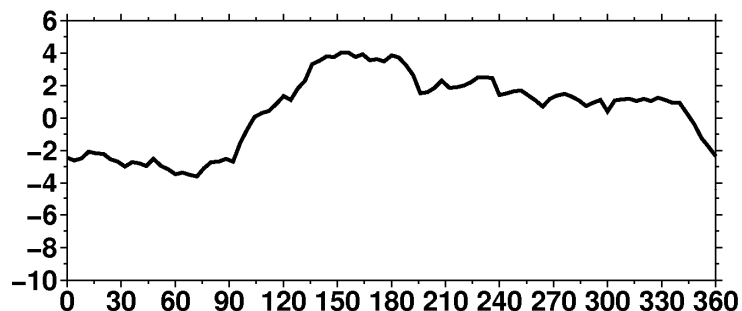
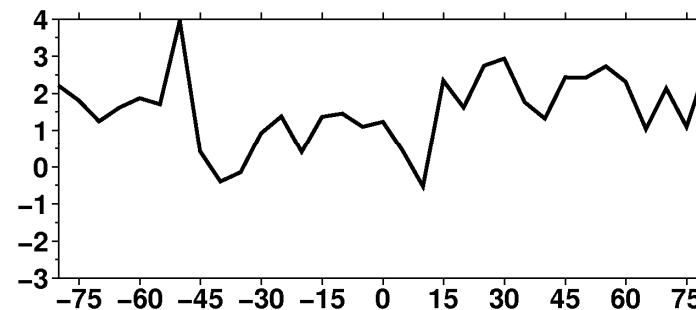
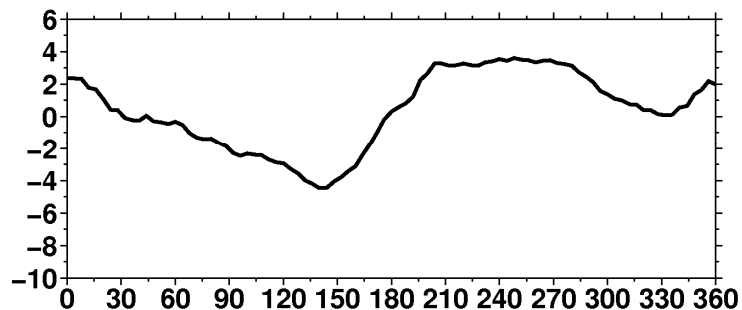
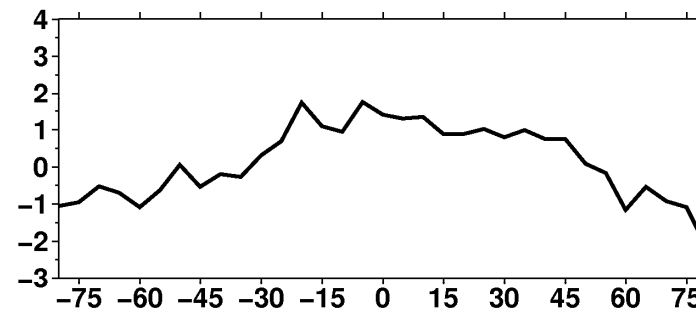
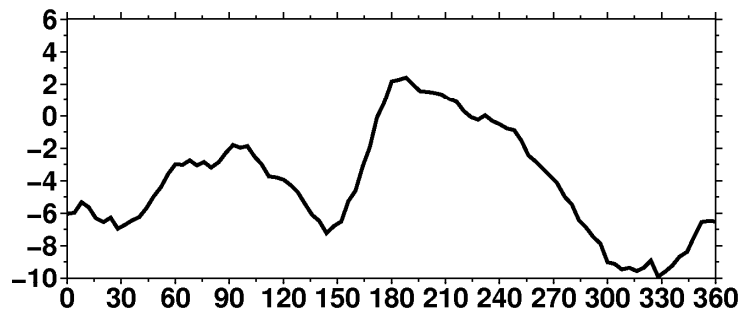
EOFs of the J1–TX cal phase differences



EOFs of J1–TX orbit – range

Solar angle basis functions

Beta angle basis functions



α' (deg)

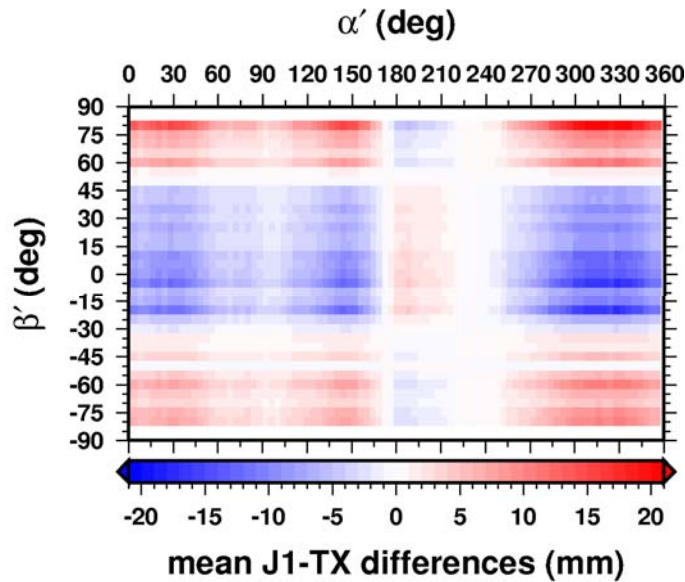
β' (deg)



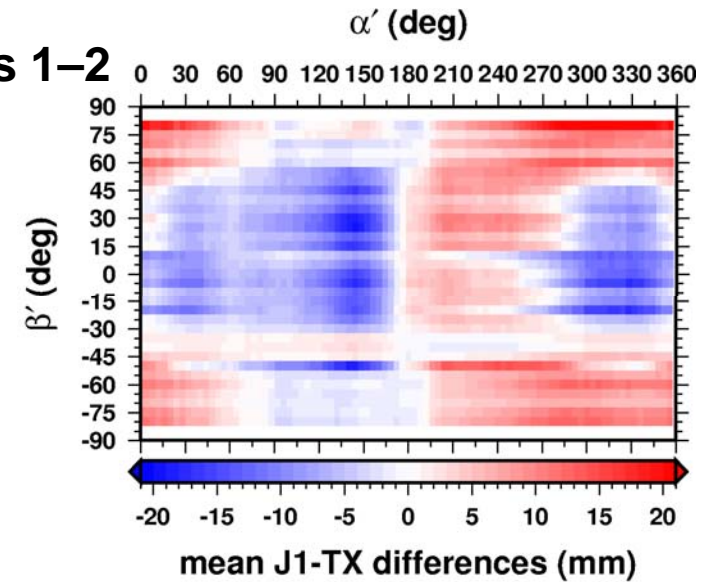
Correction from reconstruction of EOFs



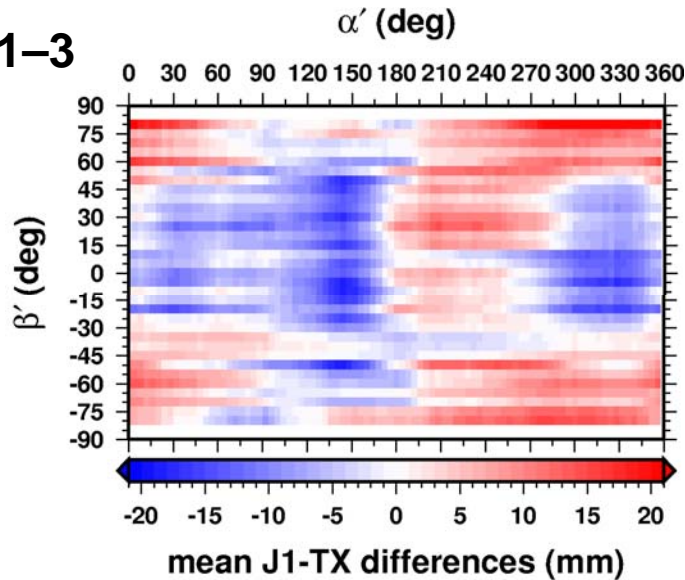
EOF 1



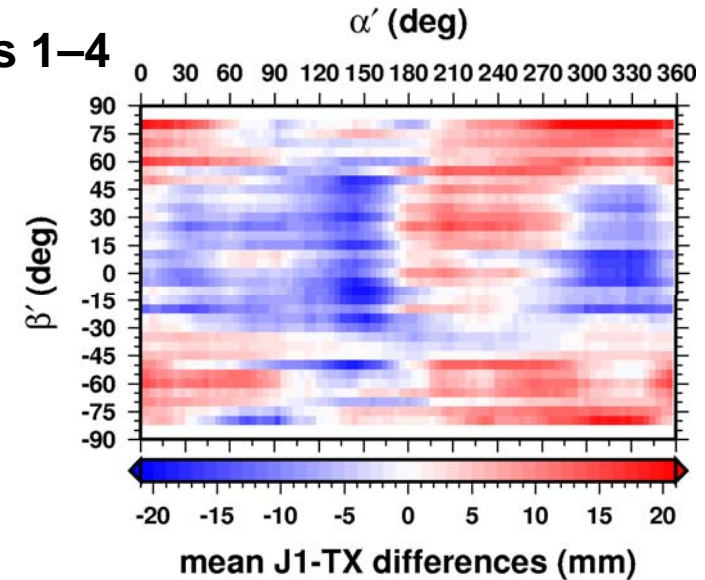
EOFs 1-2



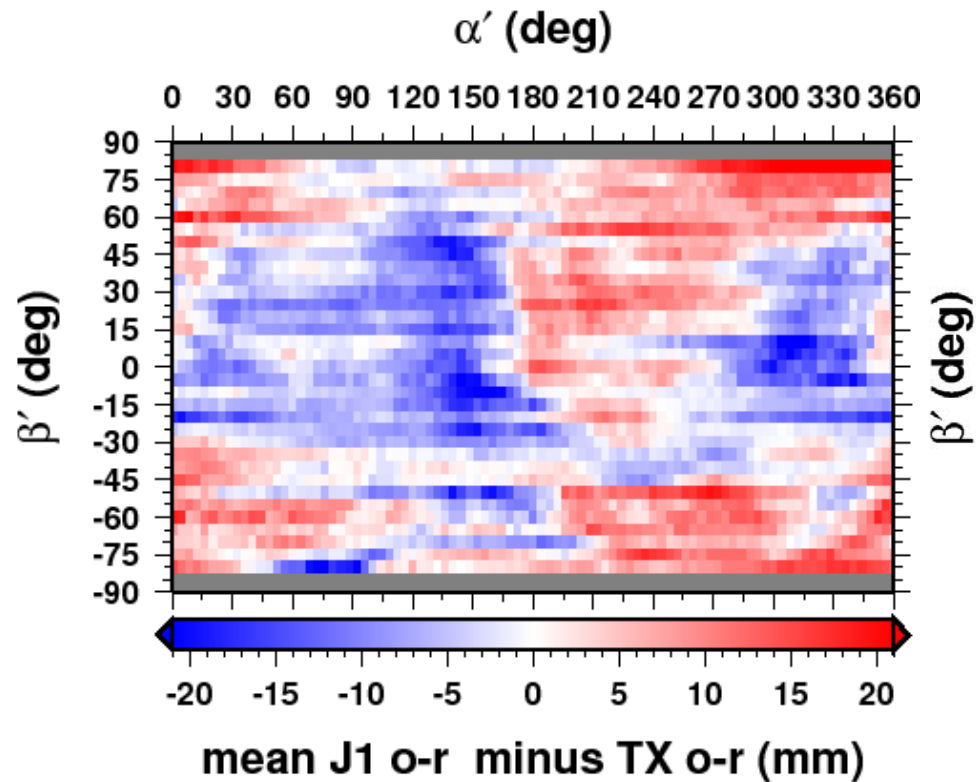
EOFs 1-3



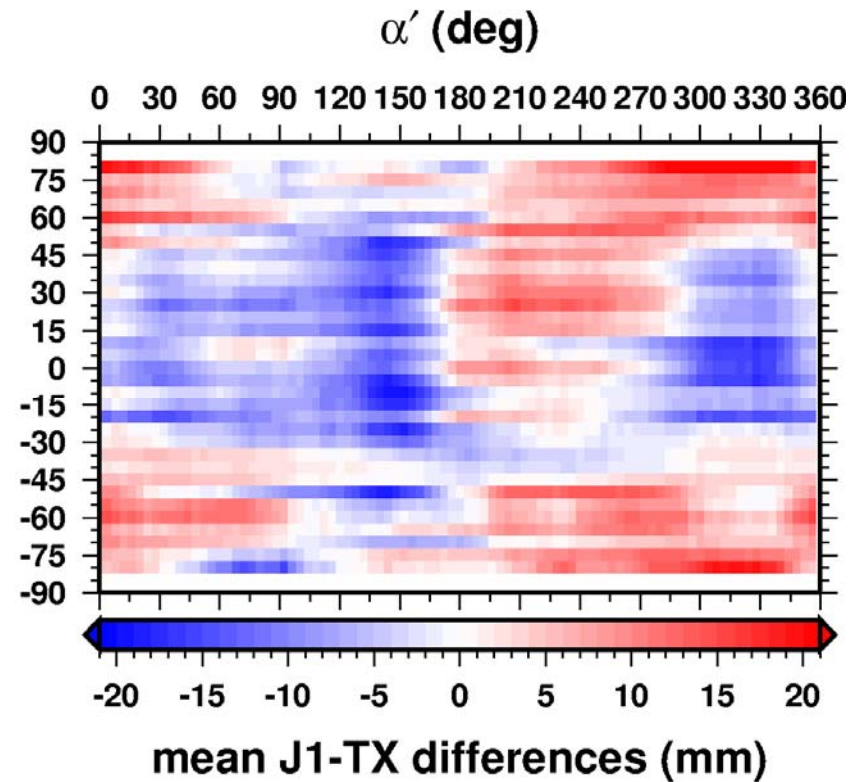
EOFs 1-4



Original differences



Reconstruction from EOFs 1-4

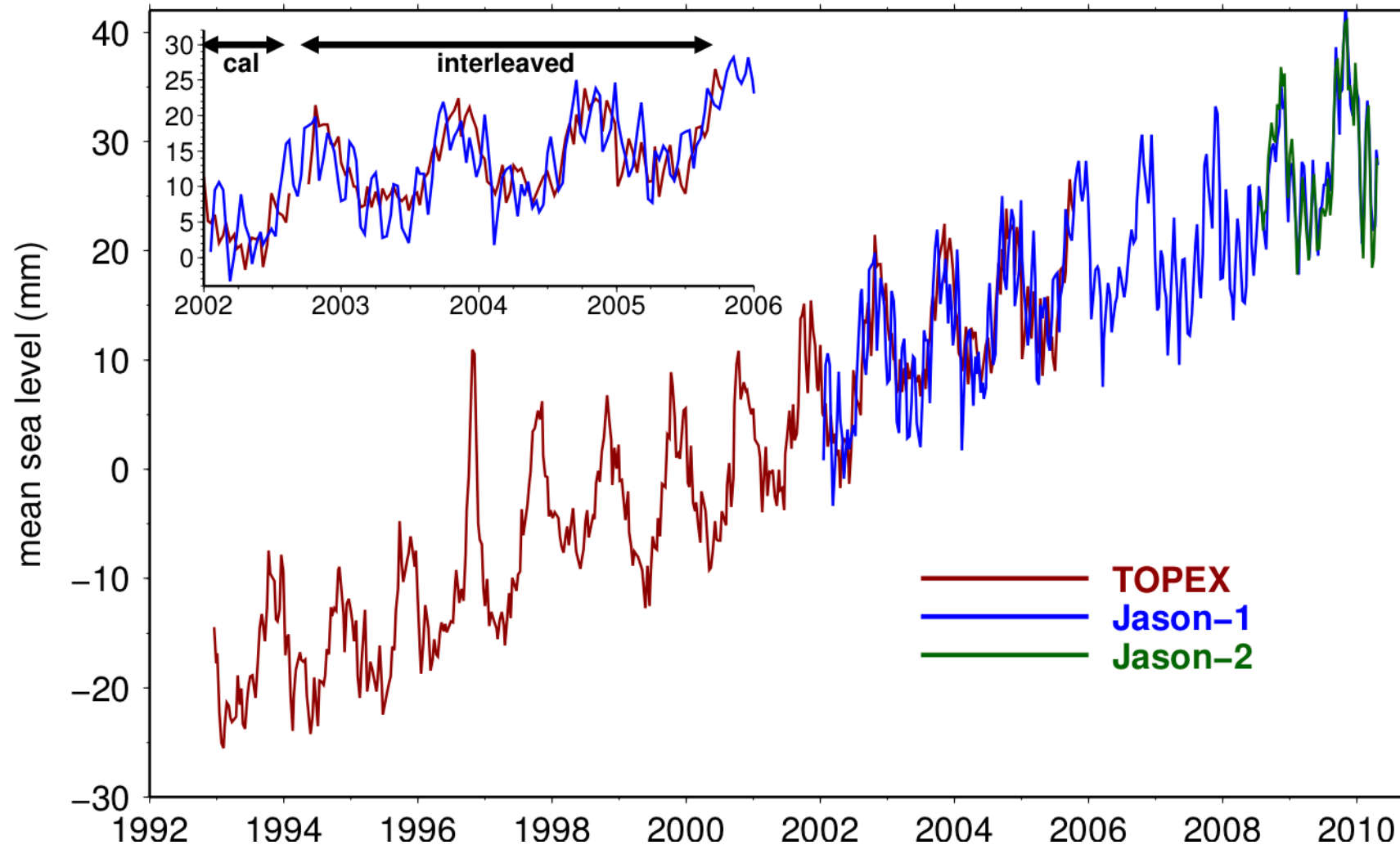




TX/J1/J2 sea level record



Uncorrected

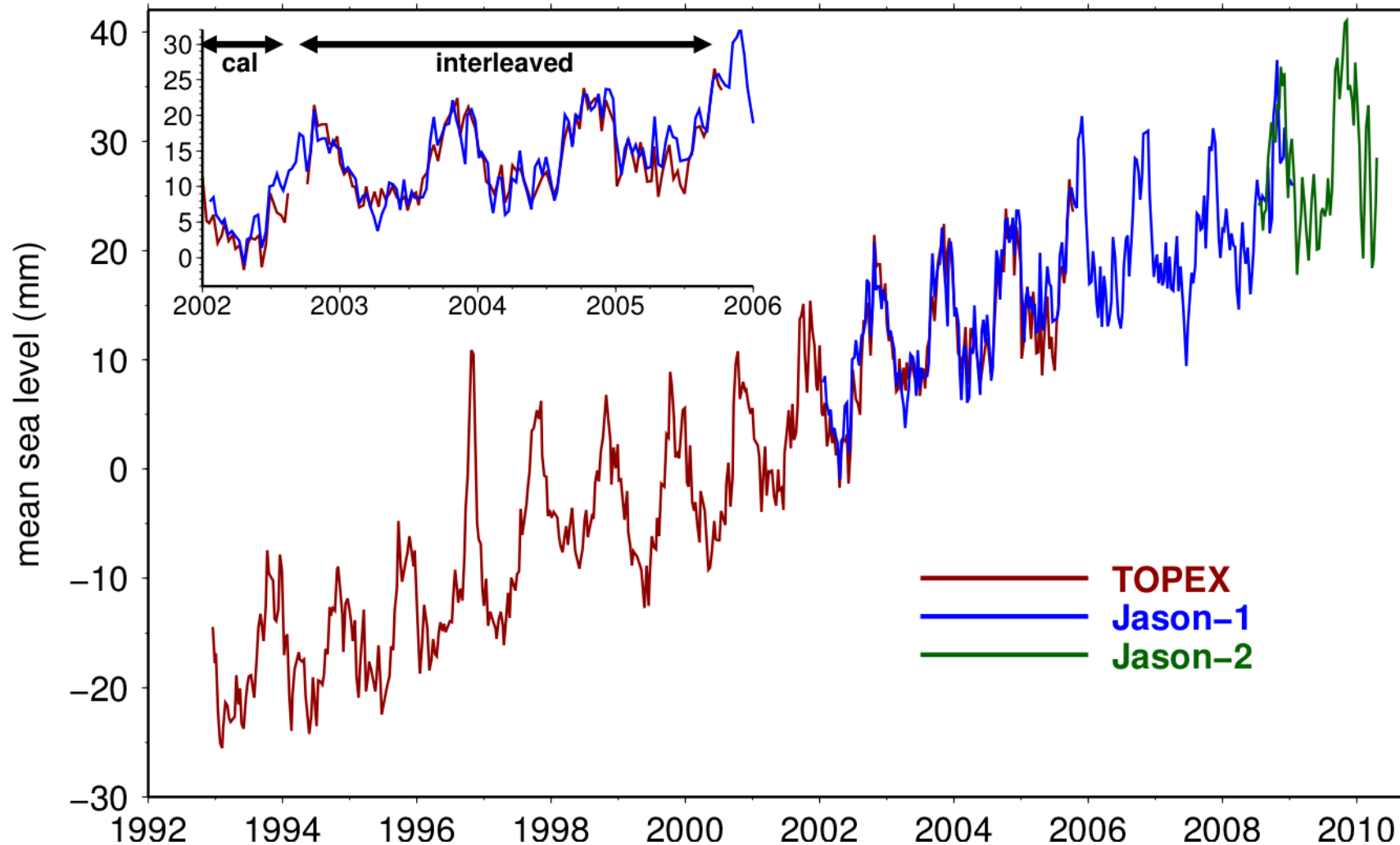




Sea level record with J1 correction



Correction EOF 1-4





Correction applied to J1–TX differences



Statics for J1—TX global mean sea level residuals during each TOPEX phase

	Calibration phase		Interleaved phase	
	St. dev. (mm)	Variance reduction	St. dev. (mm)	Variance reduction
Uncorrected	4.8		4.2	
EOF 1	2.5	73%	2.4	68%
EOFs 1–2	2.2	78%	2.2	73%
EOFs 1–3	2.0	82%	2.1	75%
EOFs 1–4	2.0	83%	2.0	77%



Correction applied to calibration phase



Amplitude of 59-day cycle in J1—TX sea level differences during the calibration phase (Jason cycles 1 – 20)

	Amplitude, 59 days (mm)	Variance reduction	Amplitude, 182.5 days (mm)
Uncorrected	5.9		1.4
EOF 1	2.6	80%	0.1
EOFs 1–2	2.2	86%	0.3
EOFs 1–3	2.0	89%	0.4
EOFs 1–4	1.9	90%	0.6



Correction applied to interleaved phase



Amplitude of 59-day cycle in J1—TX sea level differences during interleaved phase (Jason cycles 26 – 138)

	Amplitude, 59 days (mm)	Variance reduction	Amplitude, 182.5 days (mm)
Uncorrected	5.1		1.3
EOF 1	1.8	87%	0.1
EOFs 1–2	1.3	94%	0.2
EOFs 1–3	1.1	95%	0.2
EOFs 1–4	1.1	95%	0.3



Conclusions



Is the TOPEX CoG correction valid?

- Amplitude of 59-day signal is smallest when CoG & GOT4.7 applied
- Tide gauge calibration implies CoG should be applied

How does the J1–TX SSH and orbit – range bias depend on sun angle and orbital parameters?

- Coherent patterns with a range of 5 cm

Can an empirical correction based on J1–TX cal phase differences remove the 59-day & semi-annual in the J1 time series?

- A correction based on 1 or 2 EOFs reconstructing J1–TX biases during the calibration phase can nearly eliminate the 59-day signal during the entire Jason-1 mission

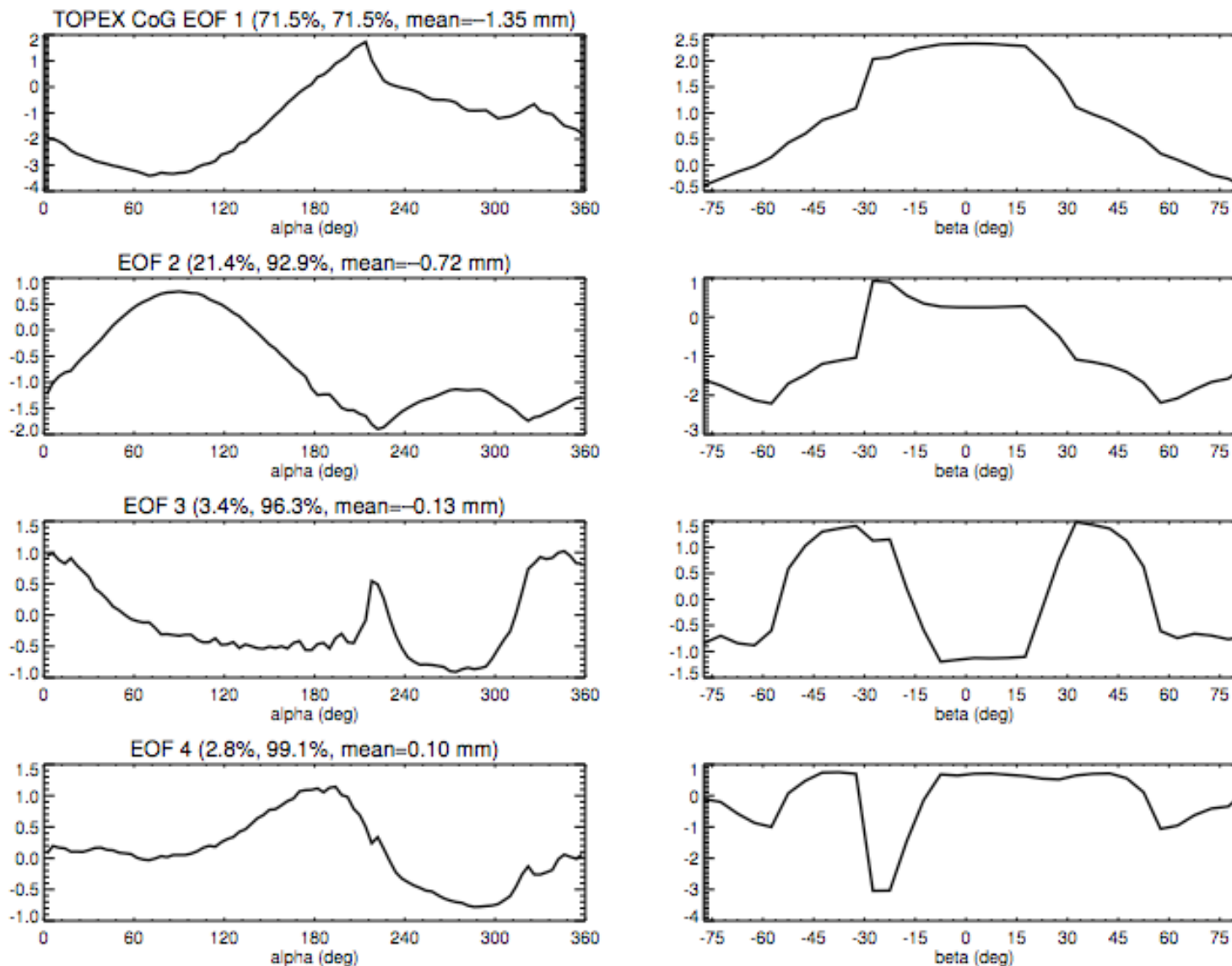


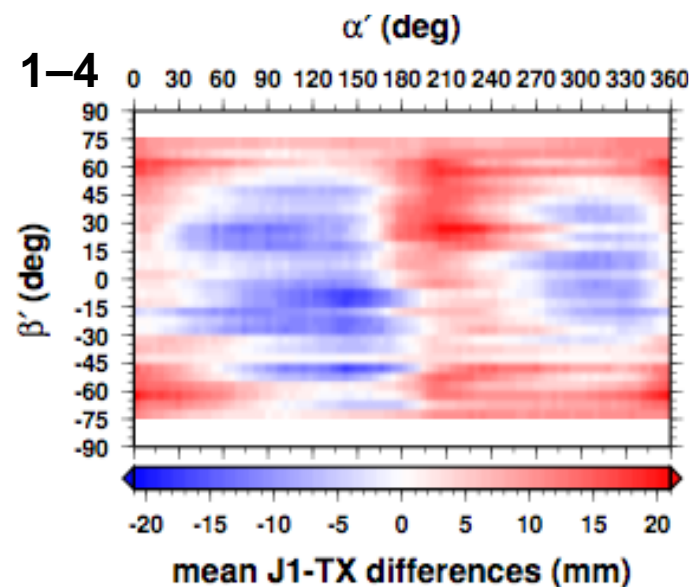
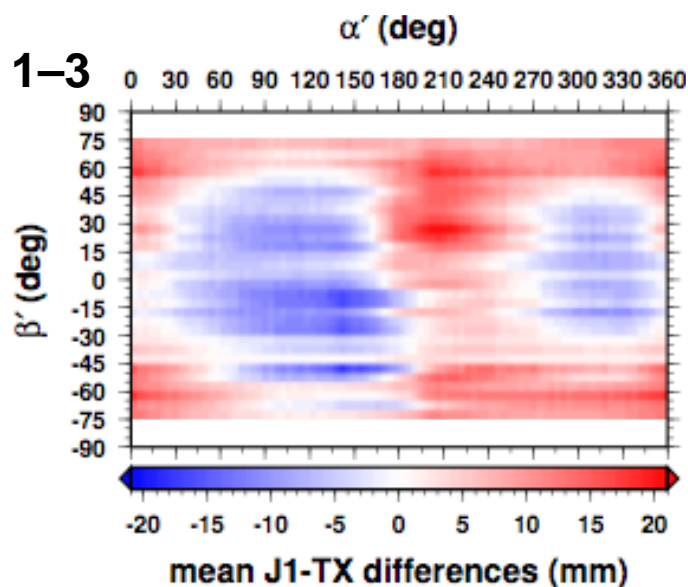
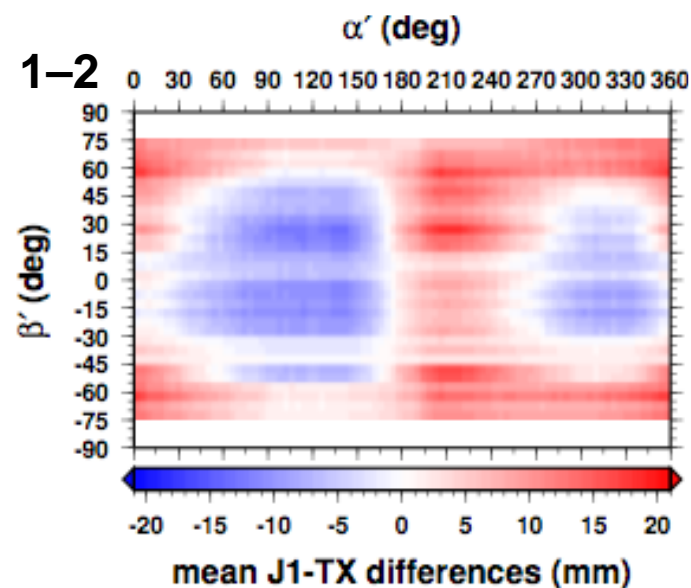
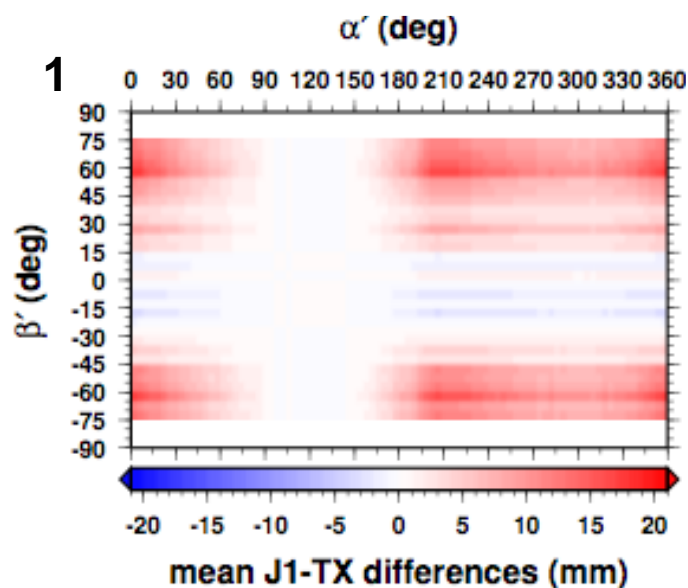
Backup slides





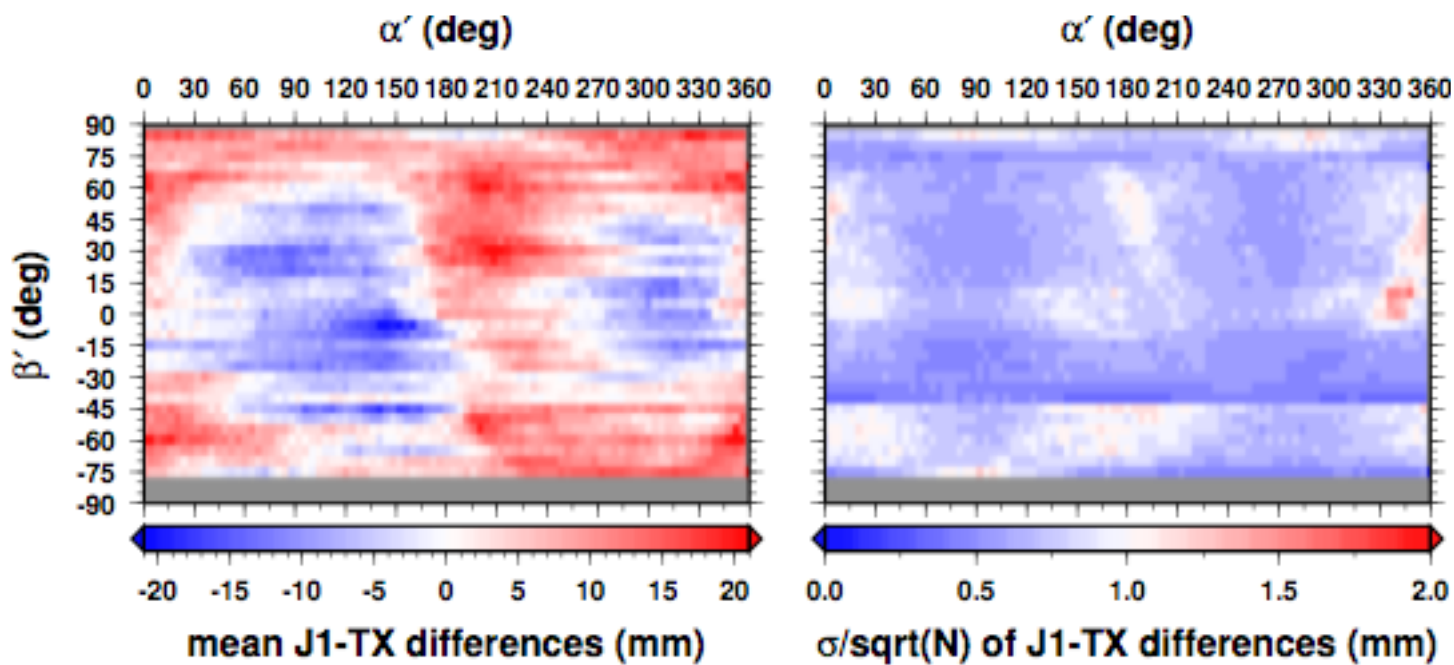
EOFs of the TOPEX CoG correction





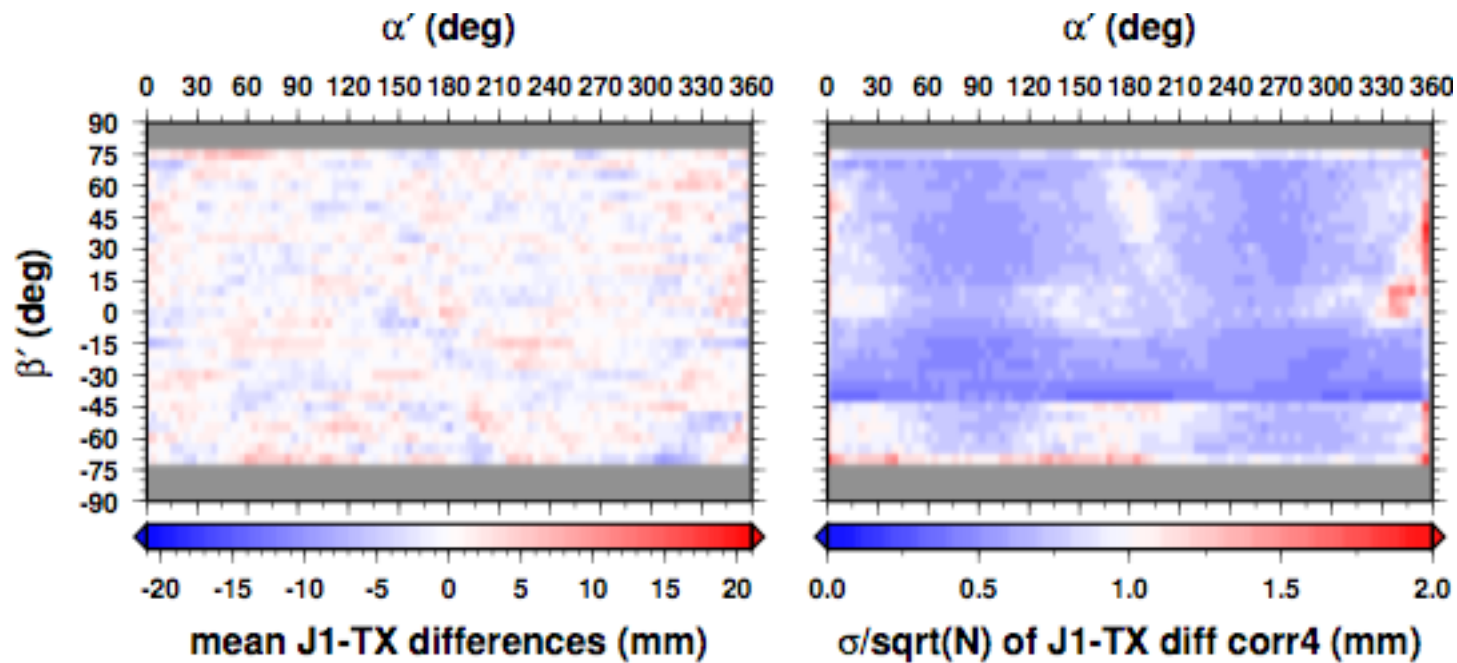


Significance of biases



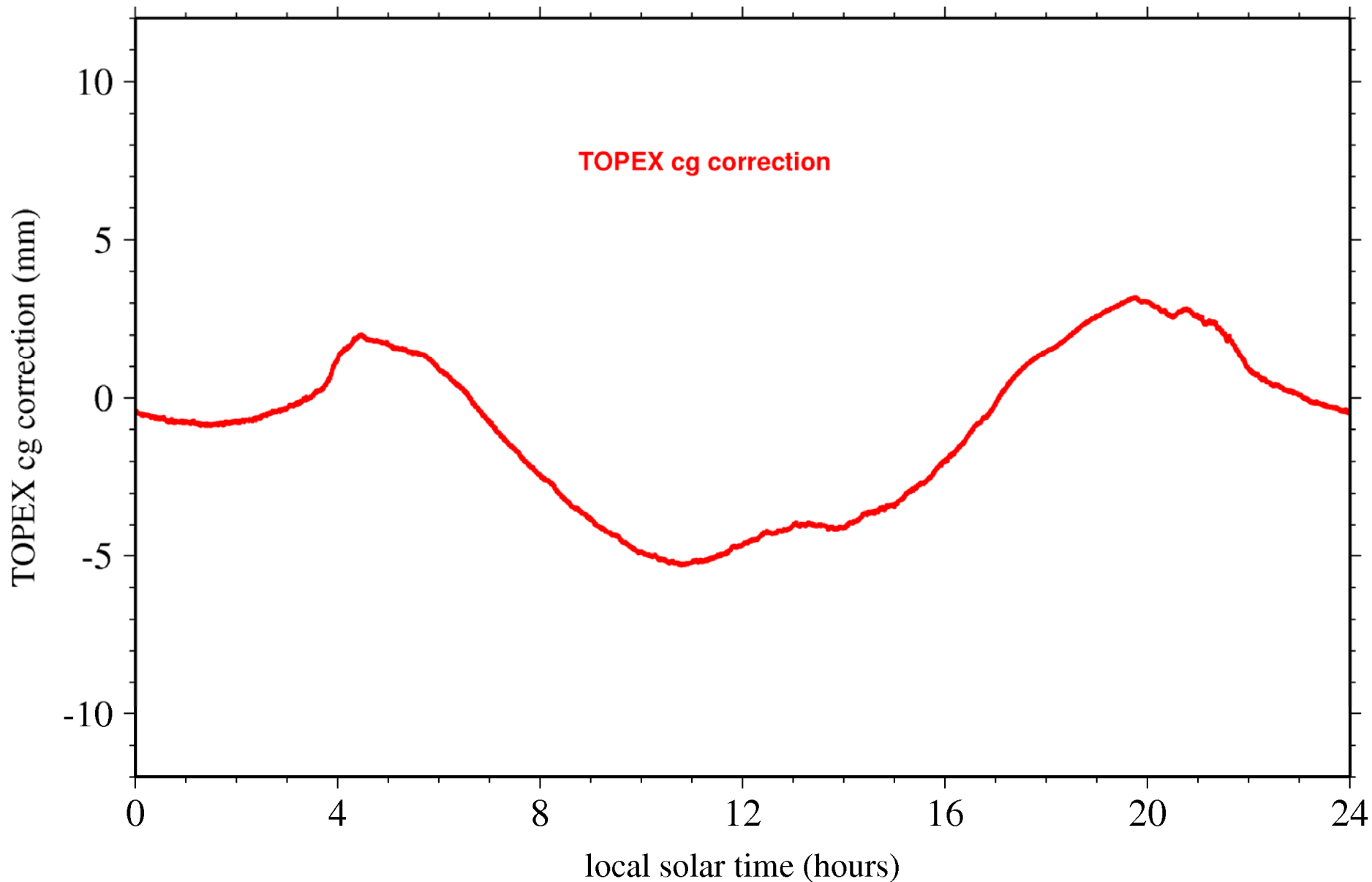


After correction applied





TOPEX CoG





Air tides

