# Southern Ocean 4-D circulation: combining altimeter and Argo float data

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## Motivation

Since the launch of the Argo program the number of observations in the Southern Ocean has steadily increase, however, some regions still remain poorly observed.

Quality controlled delayed-mode Argo profiles per 4° x 2° bins



0 25 50 75 100 125 150 175 200 225 250 275 300 325 350

Profiles per year and latitude band for 2001-2010



## Motivation

This relatively low resolution in space and time restricts the observational analysis of subsurface ACC variability to hydrographic sections, and basin or circumpolar scale studies of subsurface variability are largely model based.

### Goal

Take advantage of the close relation between subsurface density profiles and surface proxies, such as dynamic height to extract information on the subsurface structure.

## How much variance can be explained by the altimeter?



## Regression analysis: average vertical structure



Positive SSH' values indicate a depression of the isopycnals, which can in turn be driven by positive  $\Theta'$  or negative  $S_A'$ .

Therefore negative regression slopes are expected for  $S_A'$  and  $\sigma_{\theta}'$  and positive slopes for  $\Theta'$ .

Mean regression coefficients for  $\sigma_{\theta}'$ and  $\Theta'$  have the expected signs, however a sign reversal occurs for  $S_A'$  at 800 db.

#### Regression analysis: slice at 1000db



 $SSH' > 0 \longleftrightarrow \sigma_{\theta}' < 0$  $\alpha(\sigma_{\theta}) < 0$ 

 $SSH' > 0 \iff S_A' < 0$  $\rightarrow \alpha(S_A) < 0$ 

 $SSH' > 0 \iff \Theta' > 0$  $\longrightarrow \alpha(\Theta) > 0$ 

## Regression analysis: meridional sections

Regression between SSH' and  $S_A'$ - Meridional section at 45° W

.03



Regression coefficient between SSHa and SA' (cm<sup>-1</sup> g kg<sup>-1</sup>) - Meridional section at 45°W



## Example of regression analysis



## Objective mapping Estimation of the covariance matrix

Depth-averaged (100-1900db)  $\sigma_{\theta}'$  correlation (red) and Gaussian fit (black).



## Objective mapping Mean fields at 1000 and 1500db



#### Reconstructing the 4-D fields

Each variable can be objectively mapped after removing the altimeter signal:

$$\hat{\phi} = \{\phi - \alpha(\phi) * SSH'\}$$

Using the regression coefficients  $\alpha(\emptyset)$  and SSH' as a proxy, each variable can then be mapped in space and time:

$$\phi_M(x, y, z, t) = \alpha(\phi(x, y, z)) * SSH'(x, y, t)$$

The full 4-dimensional field can be reconstructed by adding the objectively mapped mean field to the mapped variable:

$$\Phi(x, y, z, t) = \hat{\phi}(x, y, z) + \phi_M(x, y, z, t)$$

# Reconstructing the 4-D fields

Indian Ocean SSH and potential density field for 2009-2010



## Dynamically constrained MDT



	SR1 Drake	SR2 Africa	SR3 Tasmania	SR1-SR2
CNES-CLS09	172 ± 6 (224)	135 ± 31 (169)	$164 \pm 4 (188)$	37 (55)
EGM08	$151 \pm 3$ (205)	$136 \pm 13$ (166)	$167 \pm 4 (194)$	15 (39)
GGM02C	$142 \pm 2 (182)$	$188 \pm 23$ (219)	$175 \pm 3 (200)$	46 (37)
MN05	$159 \pm 4$ (211)	98 ± 18 (133)	$187 \pm 7 (213)$	61 (78)
SOSE	$147 \pm 5$	$145 \pm 15$	$159 \pm 3$	2

From Griesel et al. (JGR, 2012)

Find a MDT that is consistent with the available products and some dynamical constraint by minimizing a cost-function that is the sum over all space of:

$$J = \sum_{i=1,N_{\text{MDT products}}} (\eta - \eta_{product i})^2 \sigma_{product i}^{-2} + (\eta - \eta_{vort})^2 \sigma_{vort}^{-2}$$

#### Dynamically constrained MDT

QG linear vorticity balance:

$$\beta v + u_H \cdot \nabla \zeta = f \frac{\partial w}{\partial z}$$
 (1)

From geostrophy and hydrostatic balance:

$$v = \frac{g}{f\rho_0} \int_z^0 \frac{\partial\rho}{\partial x} dz' + \frac{g}{f} \frac{\partial\eta}{\partial x}$$
(2)

Replacing (2) in (1) and integrating between the surface and some level H:

$$\frac{\beta g H}{f} \frac{\partial \eta}{\partial x} + \frac{\beta g}{f \rho_0} \int_{-H}^{0} \int_{z}^{0} \frac{\partial \rho}{\partial x} dz' dz = \frac{1}{\rho_0} \nabla \times \tau - fw(z = -H)$$

$$SOSE \text{ (next: Argo)} ECMWF$$

## Dynamically constrained MDT

$$\eta(x,y) = \eta(x_0,y) + \frac{f}{\beta g H \rho_0} \int_{x_0}^x \nabla \times \tau \, dx - \frac{f^2}{\beta g H} \int_{x_0}^x w_{-H} \, dx - \frac{1}{\rho_0 H} \int_{x_0}^x \int_{-H}^0 \int_z^0 \frac{\partial \rho}{\partial x} \, dz' \, dz \, dx$$



#### Summary

Due to the strong vertical coherence and equivalent barotropic nature of the ACC, it is possible to extract substantial information on the subsurface structure by using SSH as a proxy to infer T, S and  $\sigma_{\theta}$  anomalies.

The correlation between SSH with T, S and  $\sigma_{\theta}$  is significant (95% level) on ~75% of the 3.6 million grid cells of the domain. An improvement of the signal to noise ratio is achieved, on average the anomaly variance is reduced by 40%.

The removal of the altimeter signal from T, S and  $\sigma_{\theta}$  produces more stable and less noisy estimates of the mean fields of the Southern Ocean.

QG linear vorticity budget seems to be enough to infer SSH. Further work would prove if this dynamically constrained SSH helps improve the available MDT products and a close mass balance is reached.



## Distribution of Argo profiles II



Quality controlled delayed-mode Argo profiles per 4° x 2° bins

Rapid decay of available profiles south of the PF.

Energetic regions are the least well sampled (ACC core, BFC, Agulhas recirculation).

Pacific and Eastern side of the Indian Ocean are the most well sampled regions (Southern limb of subtropical gyres).

## Distribution of Argo profiles I

Delayed-mode Argo profiles south of 30°S from 2001-2010: +152500 profiles

Around 9% of the profiles were removed after further quality control.

Significant bias towards the second half of the record (2006-2010).

The delayed in the quality control of the Argo profiles is reflected in the number of profiles available for 2010.

#### Profiles per year and latitude band

Number of ARGO profiles per year (2001-2010)



#### Removing the altimeter signal

 $\hat{\vartheta} = \{\vartheta - \alpha . SSH\} + \overline{\alpha . SSH}$ 



## Regression analysis: SSHa-SA'

Regression coefficient between SSHa and SA' at 1000db



Slope of linear regression between SSHa and SA' in 4° x 2° bins at 1000db.

Hatched bins are not significant at the 95% level.

Mean positions of fronts is shown in white and black dots show the available observations.

## Regression analysis: SSHa-CT' and SSHa- $\sigma_{\theta}'$

Regression coefficient between SSHa and CT' at 1000db

Regression coefficient between SSHa and  $\sigma_{\theta}'$  at 1000db



## Example of regression analysis II



## How much variance can be explained by the altimeter?



## Regression analysis: structure of zonal average

#### Fraction of cells with significant regression at the 95% level

20 50 0.9 80 0.8 110 140 0.7 170 200 0.6 400 0.5 600 0.4 800 Pressure (db) 1000 1200 0.3 0.2 1400 1600 0.1 1800 -70 -68 -66 -64 -62 -60 -58 -56 -54 -52 -50 -48 -46 -42 -40 -38 -36 -34 -32 -30 \_44 Latitude

Fraction of cells where regression between SSHa and  $\sigma_{a}$ ' is significant at the 95% level.