

Interactions between ocean scientists and ML scientists: timeliness and instruments in the context of SWOT ?

SWOT ST meeting
Bordeaux, 19 juin, 2019

R. Fablet

ronan.fablet@imt-atlantique.fr



#0 old friends

Empirical Orthogonal Functions and Statistical Weather Prediction

by
EDWARD N. LORENZ

MASSACHUSETTS INSTITUTE OF TECHNOLOGY
DEPARTMENT OF METEOROLOGY
Cambridge, Massachusetts

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STATISTICAL FORECASTING PROJECT

EDWARD N. LORENZ

Discusses
EOF

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Deterministic Nonperiodic Flow¹

EDWARD N. LORENZ

Massachusetts Institute of Technology

(Manuscript received 18 November 1962, in revised form January 1963)

ABSTRACT

Finite systems of deterministic ordinary nonlinear differential equations may be designed to represent forced dissipative hydrodynamic flow. Solutions of these equations can be identified with trajectories in phase space. For those systems with bounded solutions, it is found that nonperiodic solutions are ordinarily unstable with respect to small modifications, so that slightly differing initial states can evolve into considerably different states. Systems with bounded solutions are shown to possess bounded numerical solutions. A simple system representing cellular convection is solved numerically. All of the solutions are found to be unstable, and almost all of them are nonperiodic.

The feasibility of very-long-range weather prediction is examined in the light of these results.

1. Introduction

Certain hydrodynamical systems exhibit steady-state flow patterns, while others oscillate in a regular periodic fashion. Still others vary in an irregular, seemingly haphazard manner, and, even when observed for long periods of time, do not appear to repeat their previous history.

These modes of behavior may all be observed in the familiar rotating-basin experiments, described by Fultz, *et al.* (1959) and Hide (1958). In these experiments, a cylindrical vessel containing water is rotated about its axis, and is heated near its rim and cooled near its center in a steady symmetrical fashion. Under certain conditions the resulting flow is as symmetric and steady as the heating which gives rise to it. Under different conditions a system of regularly spaced waves develops, and progresses at a uniform speed without changing its shape. Under still different conditions an irregular flow pattern forms, and moves and changes its shape in an irregular nonperiodic manner.

Lack of periodicity is very common in natural systems, and is one of the distinguishing features of turbulent flow. Because instantaneous turbulent flow patterns are so irregular, attention is often confined to the statistics of turbulence, which can be compared with the turbulence, often believed to be chaotic, in a similar manner. The short-range prediction of the weather is forced willy-nilly to predict the tail of the distribution of scale turbulent eddies—the cyclones and anticyclones—which continually arrange themselves into new patterns.

¹The research reported in this work has been sponsored by the Geophysics Research Directorate of the Air Force Cambridge Research Center, under Contract No. AF 19(604)-4969.

Thus there are occasions when more than the statistics of irregular flow are of very real concern.

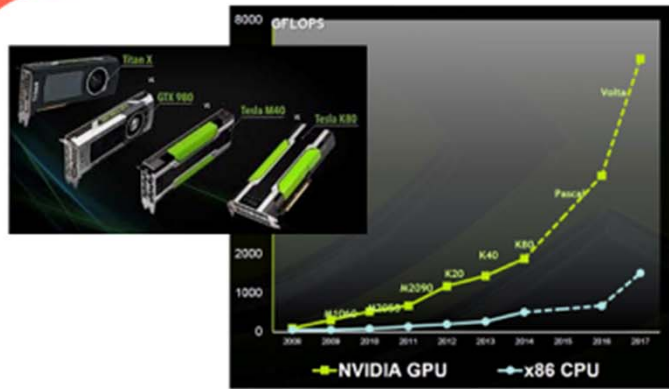
In this study we shall work with systems of deterministic equations which are idealizations of hydrodynamical systems. We shall be interested principally in nonperiodic solutions, i.e., solutions which never repeat their past history exactly, and where all approximate repetitions are of finite duration. Thus we shall be involved with the ultimate behavior of the solutions, as opposed to the transient behavior associated with arbitrary initial conditions.

A closed hydrodynamical system of finite mass may ostensibly be treated mathematically as a finite collection of molecules—usually a very large finite collection—in which case the governing laws are expressible as a finite set of ordinary differential equations. These equations are generally highly intractable, and the set of molecules is usually approximated by a continuous distribution of mass. The governing laws are then expressed as a set of partial differential equations, containing such quantities as velocity, density, and pressure as dependent variables.

It is sometimes possible to obtain particular solutions of these equations analytically, especially when the solutions are periodic or nearly periodic with time, and, in such cases, the solutions are evolved to obtain such solutions by the method of characteristics. Ordinarily, however, the solutions of these equations do not readily be determined by such procedures. Such procedures involve replacing the continuous variables by a new finite set of functions of time, which may perhaps be the values of the continuous variables at a chosen grid of points, or the coefficients in the expansions of these variables in series of orthogonal functions. The governing laws then become a finite set of ordinary differential

Analog

#1 The technology is ready (and easy-to-use)



High-performance computing (GPU)



Large annotated dataset (> 1M)

+



Efficient & easy-to-use libraries

End-to-end learning

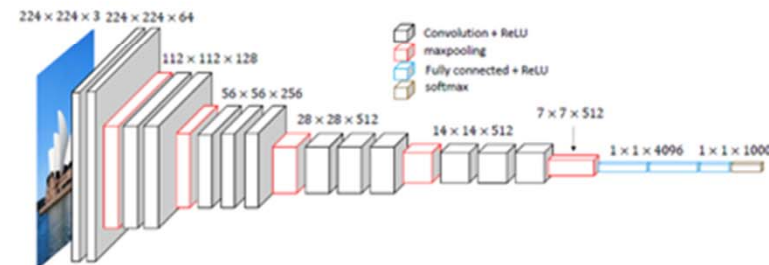


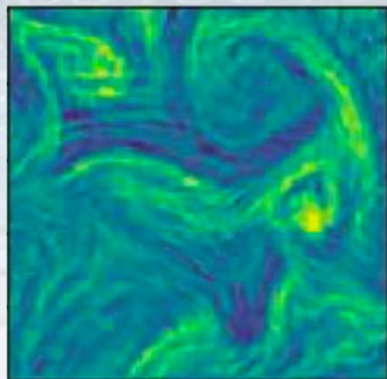
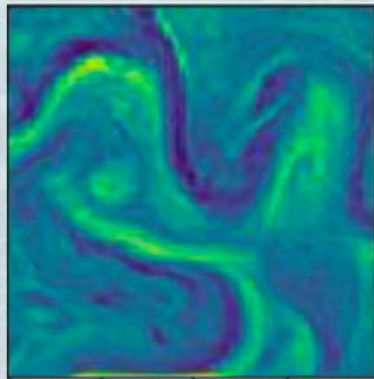
Figure 2: The architecture of VGG16 model .

136.10⁶ parameters

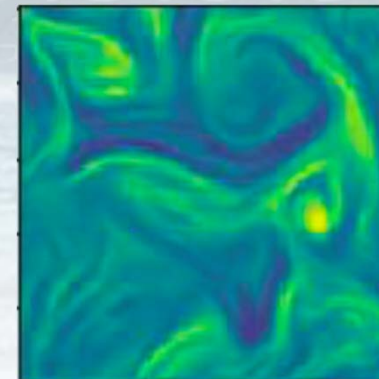
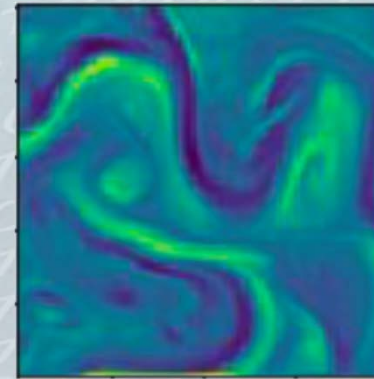
#2 Plug-and-play use of end-to-end learning

Learning-based «Noise» removal in HR snapshots (here, Laplacian of SSH fields, Osmosis region)

HR snapshots



« Denoised » tide-free output



#3 Beyond black boxes: Physics-informed learning-based representations

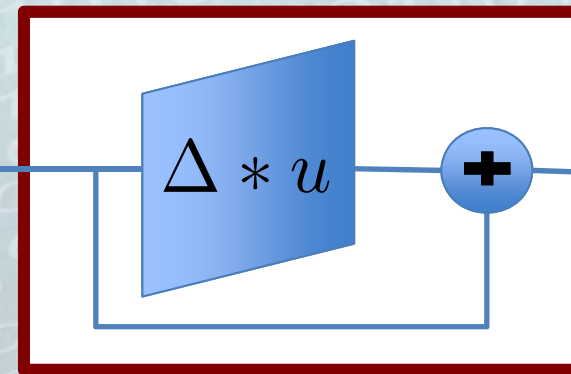
PDE/ODE

$$\frac{\partial u}{\partial t} = \kappa \Delta u$$



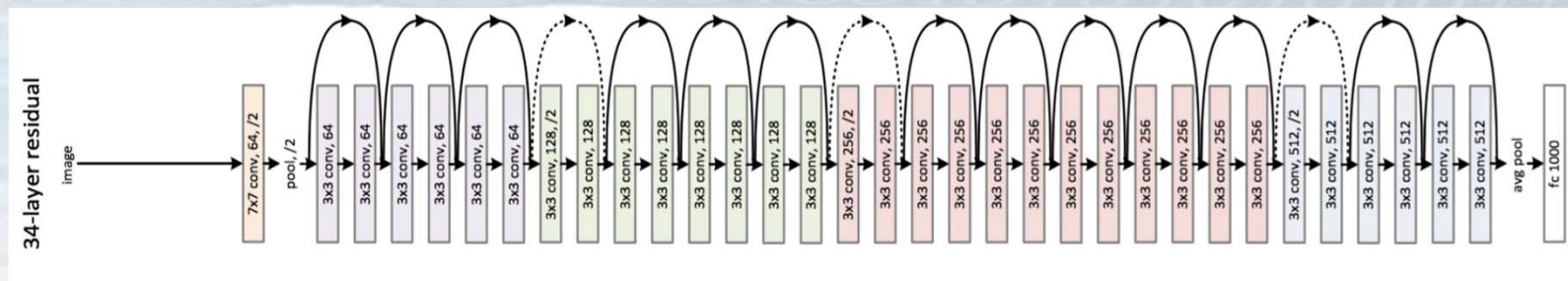
NN representation

$u(t)$

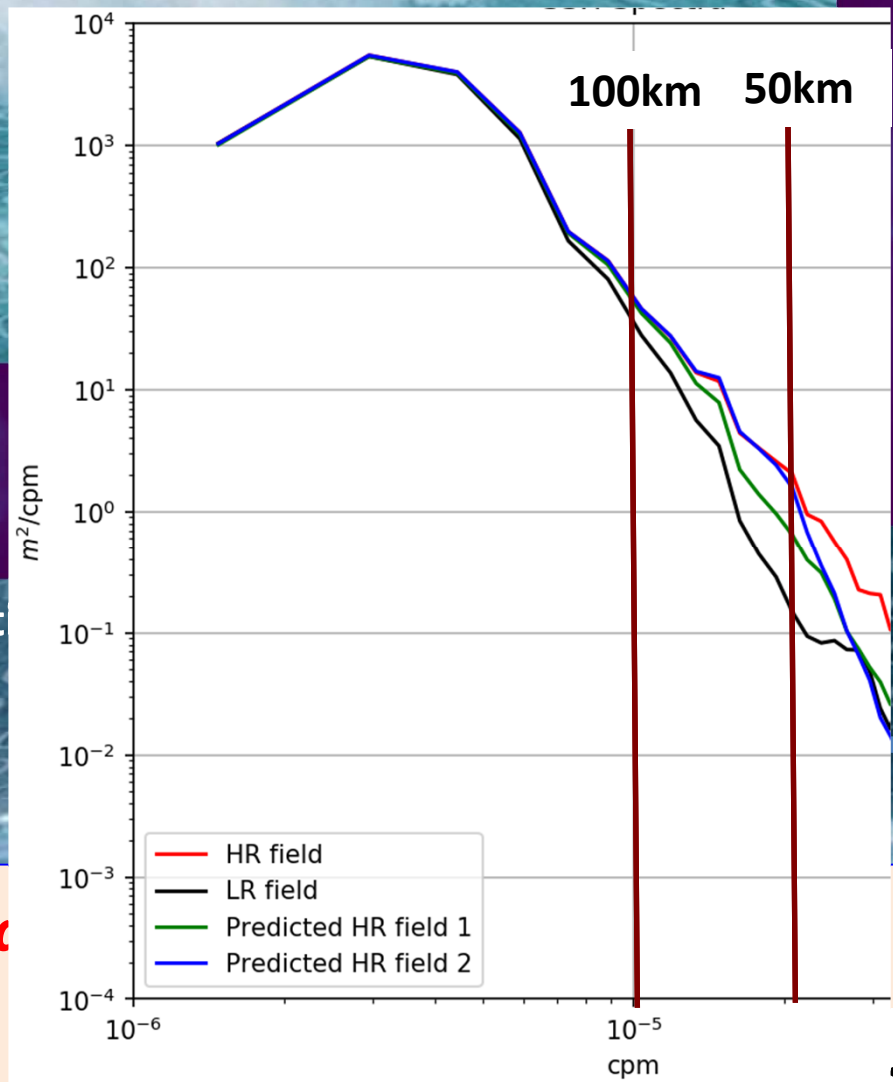


$u(t + 1)$

Numerical integration schemes as ResNets [He et al. 2015]



Learning-based Downscaling for Ocean Currents [Fablet et al., 2019]



High-resolution
($1/20^\circ$)

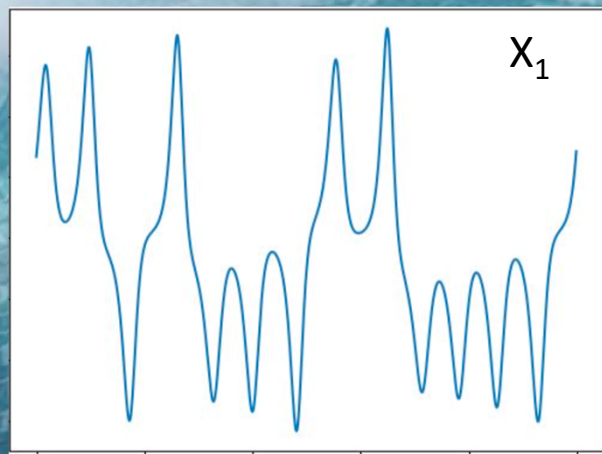
Low-resolution
($\sim 1/4^\circ$)

Subgrid-scale
variance

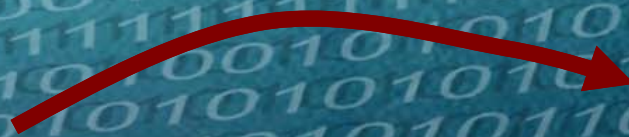
Can we learn

$\psi(X)$

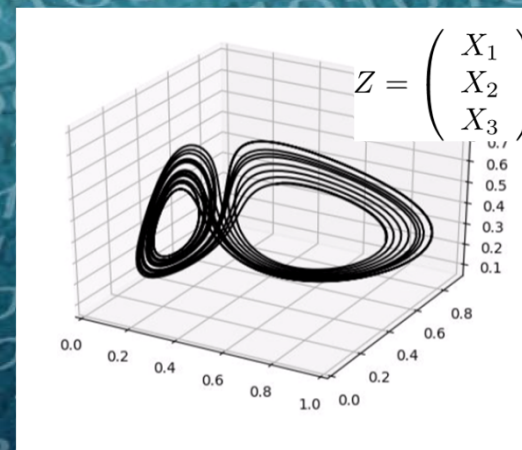
Learning latent dynamics for partially-observed systems [Ouala et al., 2019]



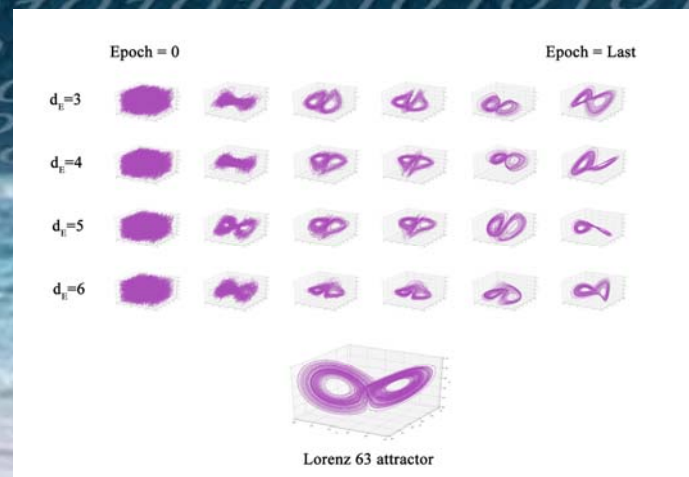
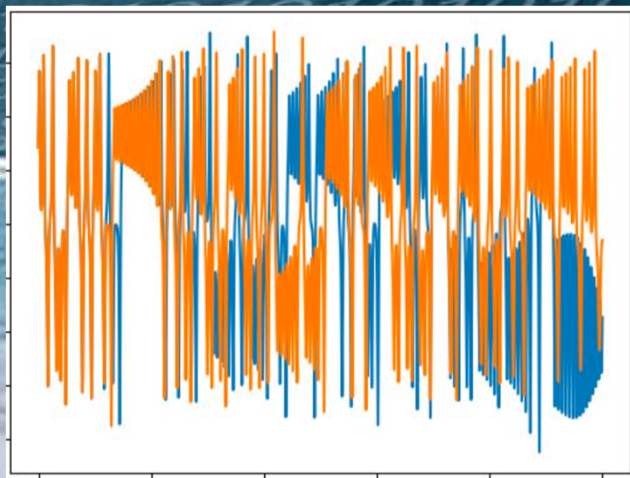
Latent (unobserved) dynamics



$$d_t Z_t = \Phi_\theta(Z_t)$$

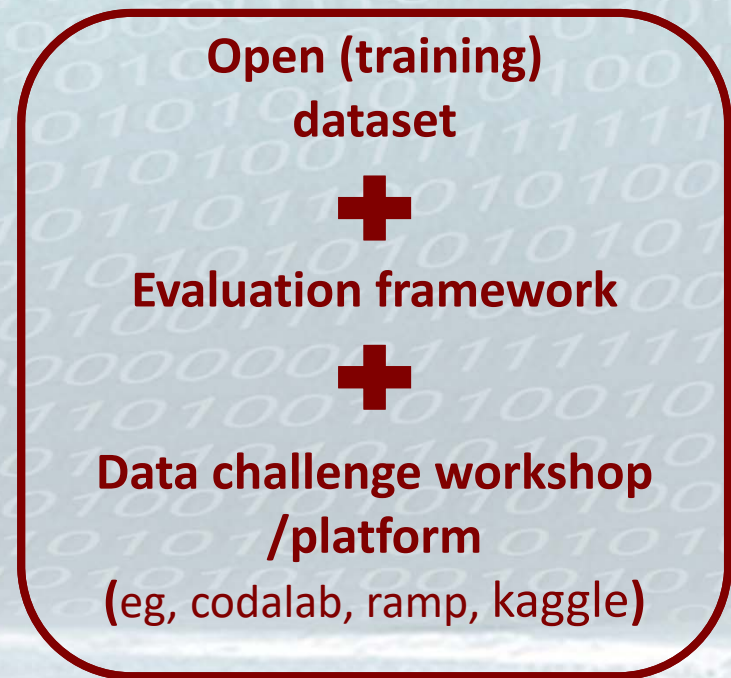
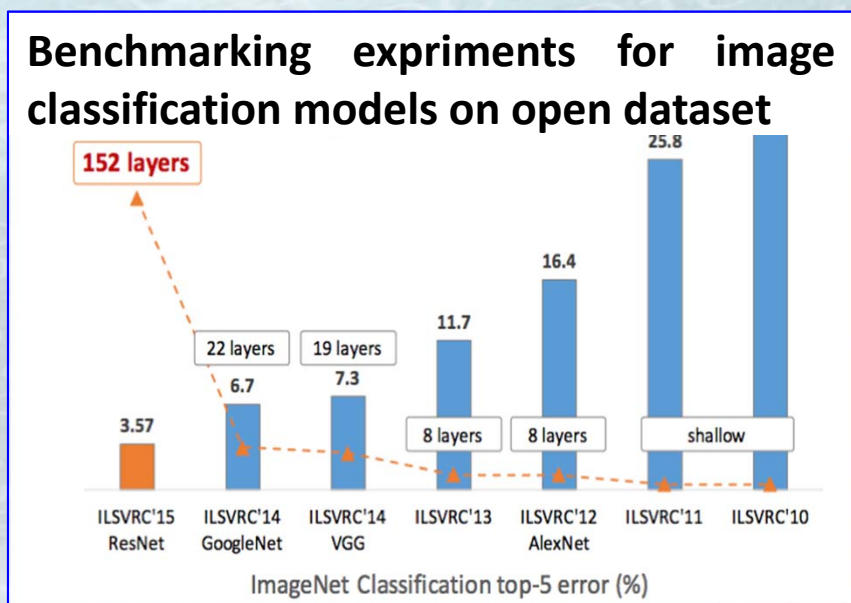


Realistic « long-term » simulations



Bridging ocean science & DL/ML: Data challenges as a key instrument ?

Shared benchmarking datasets/platforms to accelerate ML/DL breakthroughs



Relevant for ocean/swot challenges ?

Means to draw data scientists' interest ?

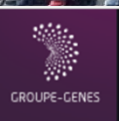
Thank you.

Lopez Radcenco et al., Analog Data Assimilation of Along-Track Nadir and Wide-Swath SWOT Altimetry Observations in the Western Mediterranean Sea. IEEE JSTARS, 2019.

Ouala et al. Neural Network Based Kalman Filters for the Spatio-Temporal Interpolation of Satellite-Derived Sea Surface Temperature. RS, 2018.

Ouala et al., Learning Latent Dynamics for Partially Observed Systems. Preprint, 2019.

More at https://www.researchgate.net/profile/Ronan_Fablet



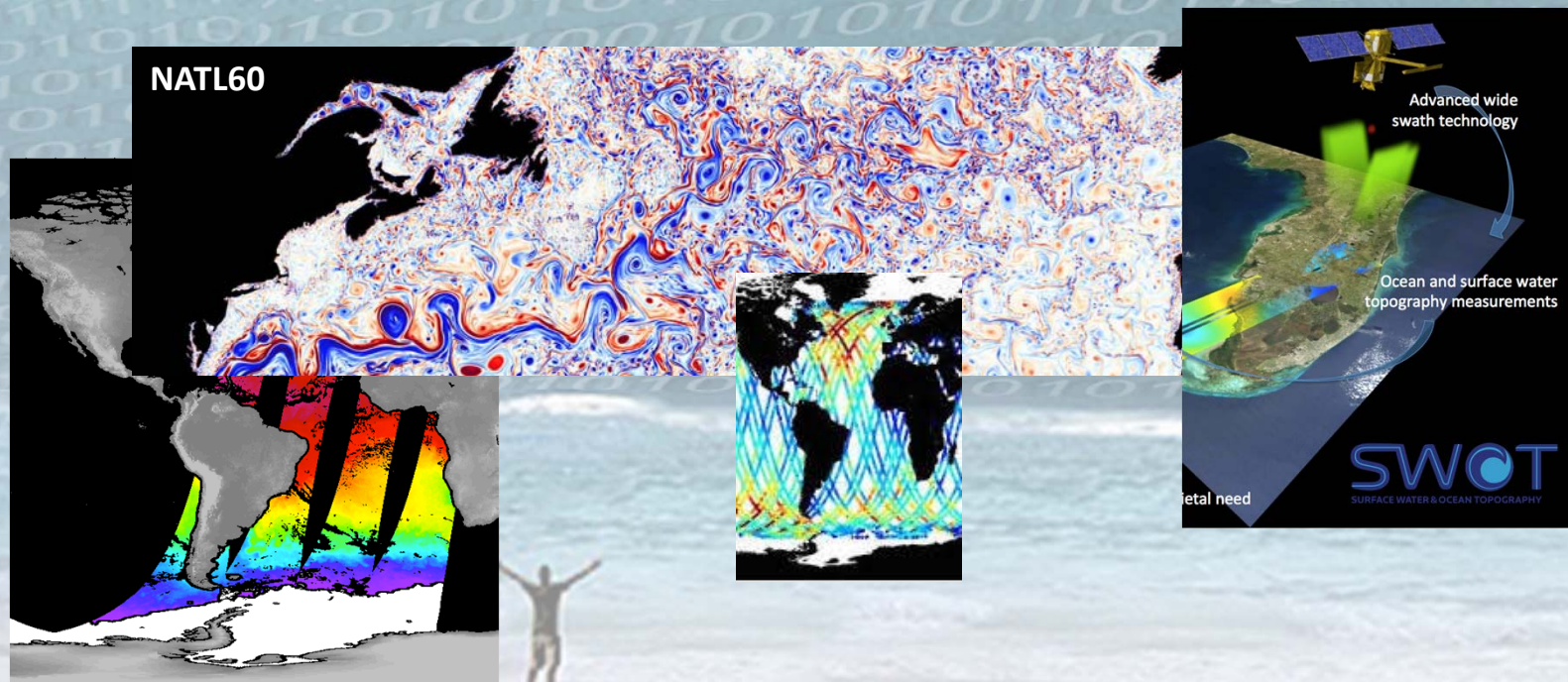
TERALAB



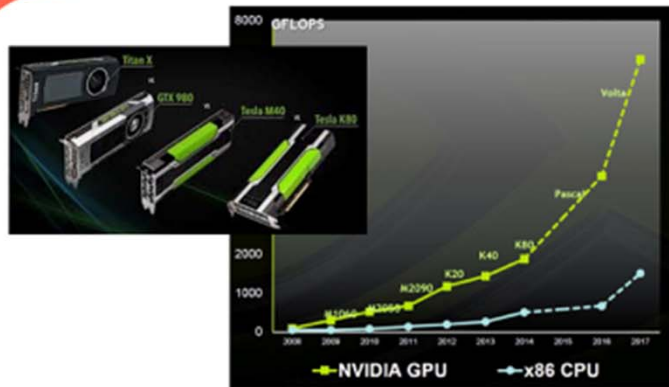
The example of analog methods. Nothing new?

Recent revival and extension of analog methods:

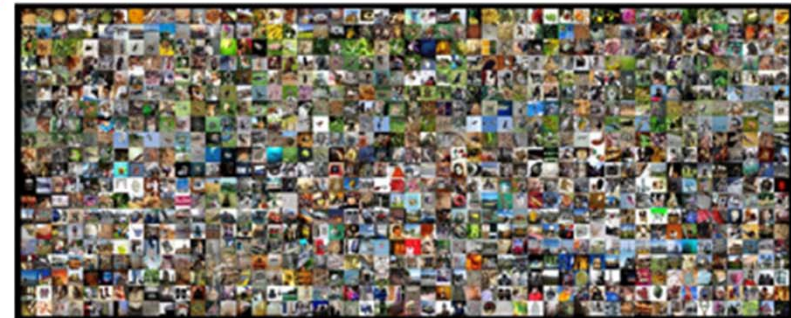
- *Downscaling, forecasting (eg, Shenk & Zorita, 2012)*
- *Analog data assimilation (Lguensat et al., 2017)*
- *Extension to geophysical fields (Fablet et al., 2017)*



Deep learning models



High-performance computing (GPU)



Large annotated dataset (> 1M)

+



Efficient & easy-to-use libraries

End-to-end learning

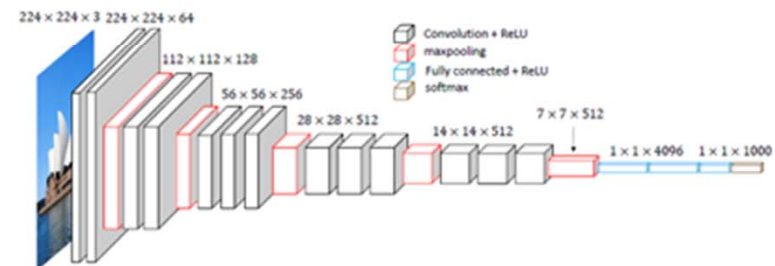


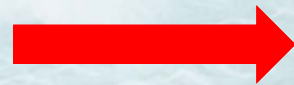
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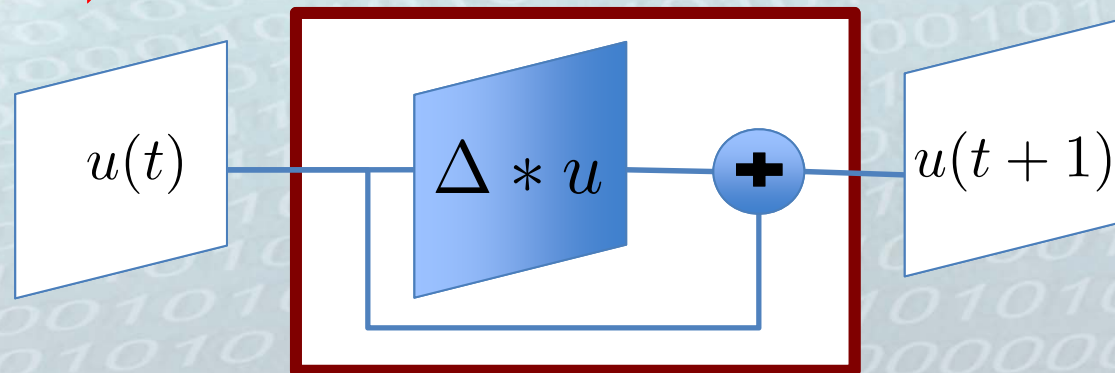
DL representations for ODEs/PDEs

PDE/ODE

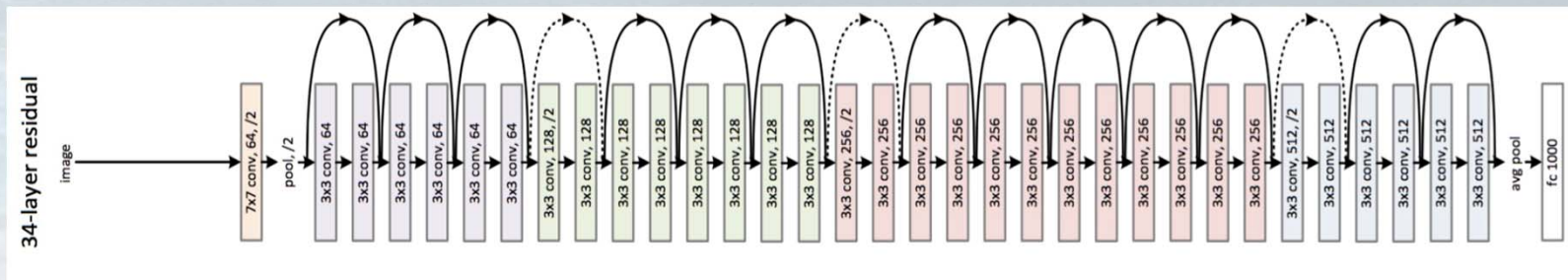
$$\frac{\partial u}{\partial t} = \kappa \Delta u$$



NN representation

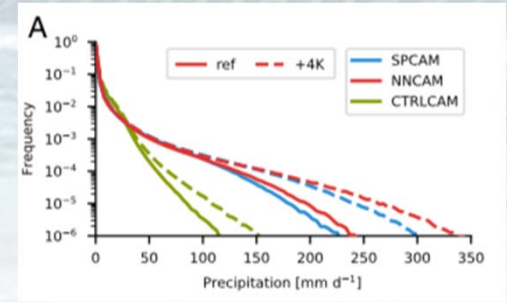
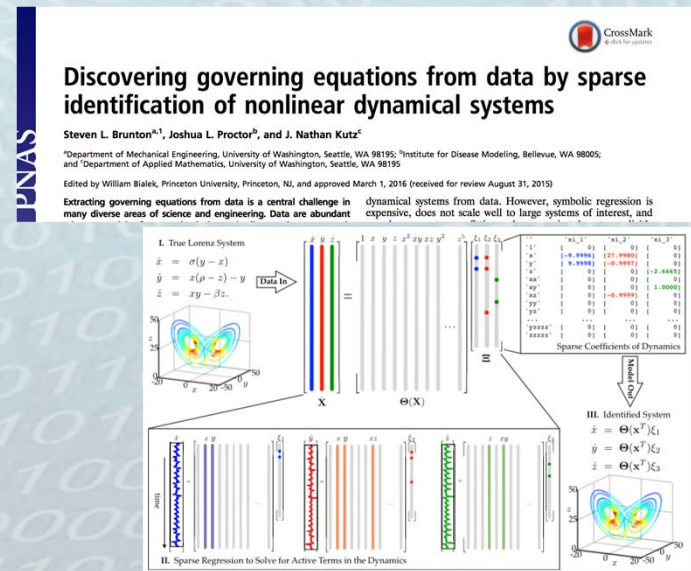


Numerical integration schemes as ResNets [He et al. 2015]

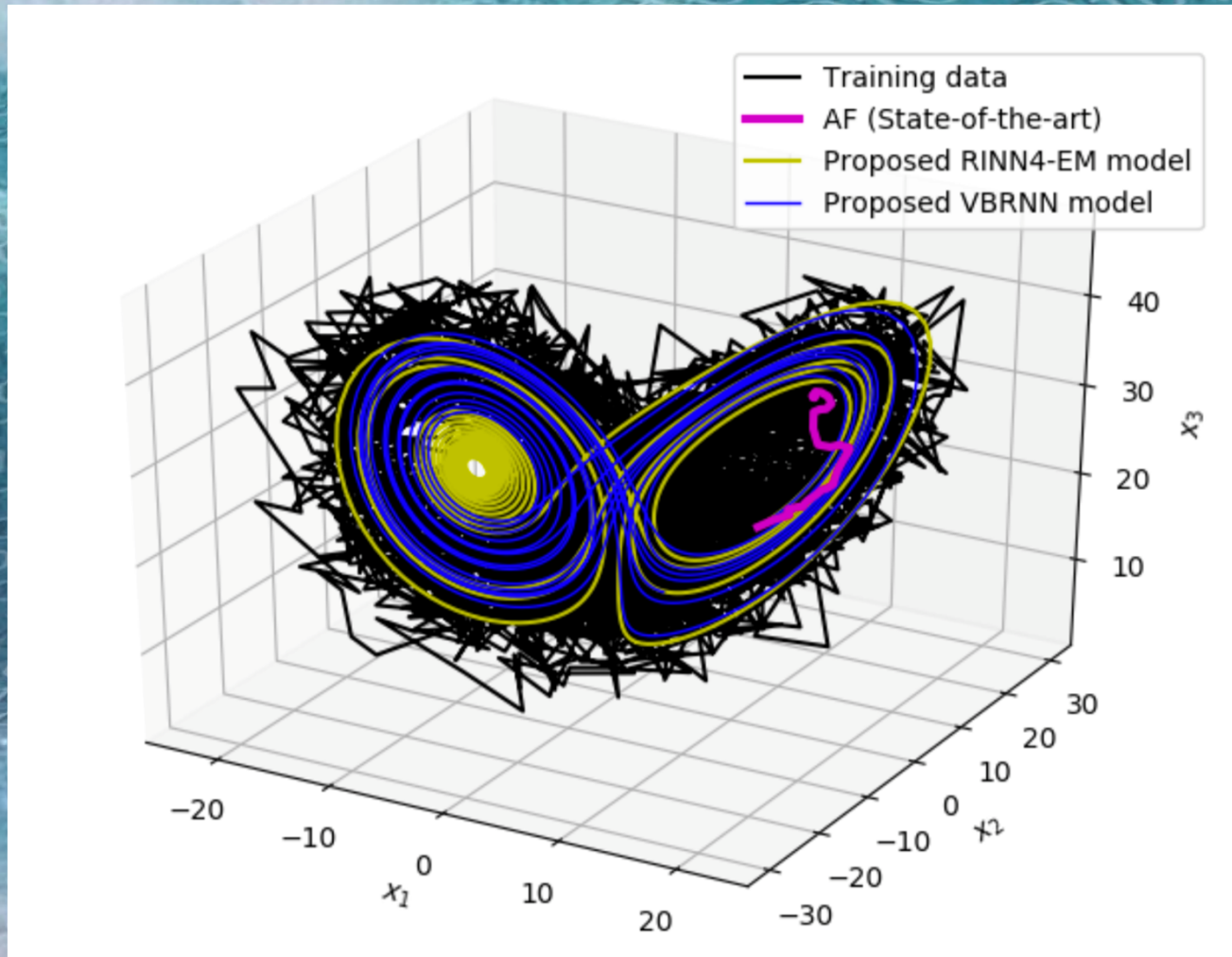


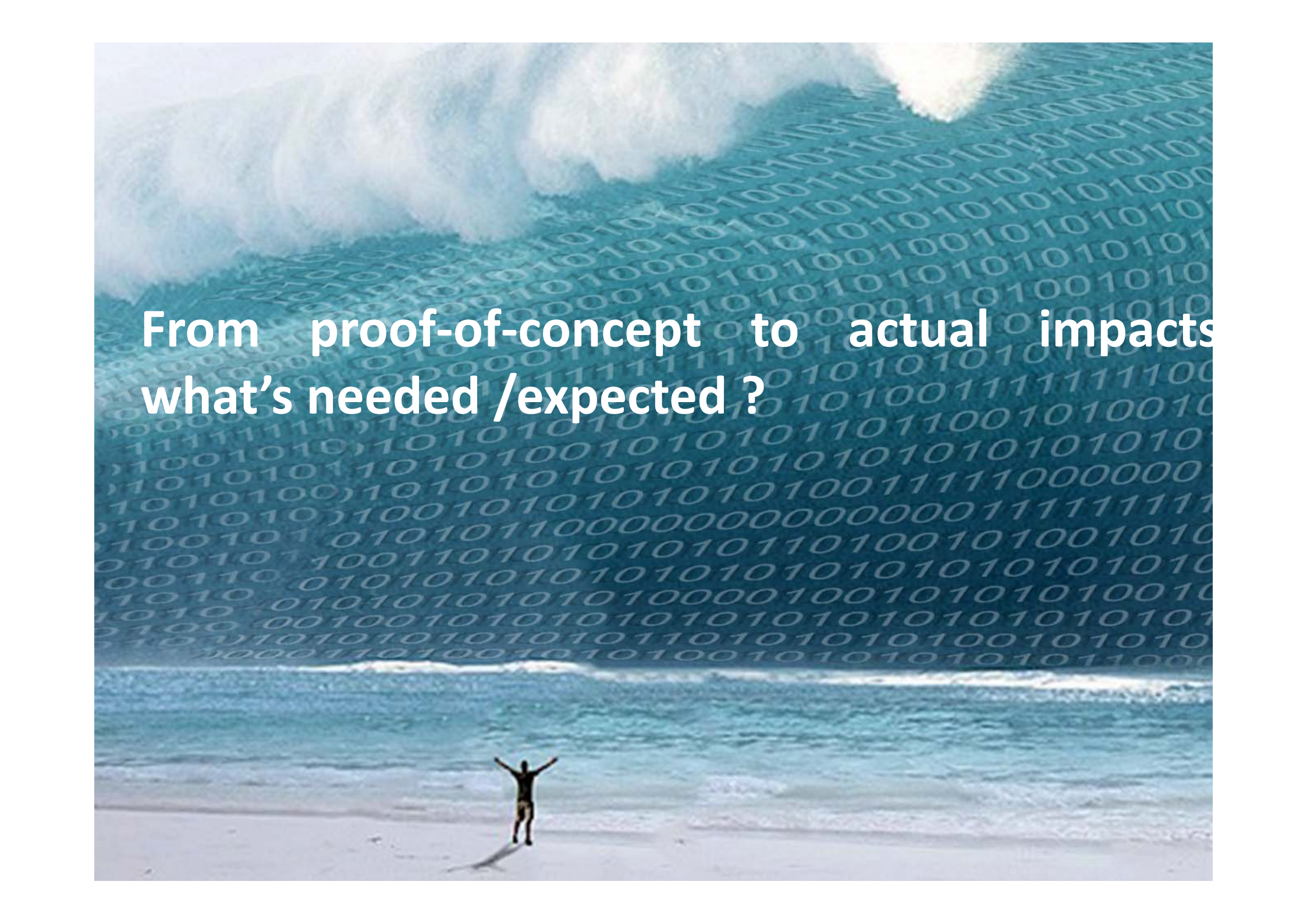
So what ? Exploring open and new challenges from a AI viewpoint

- Identification of governing equations
- Computationally-efficient models
- Improved forecasting & reconstruction
- Autonomous/adaptive observing systems



Learning from observation data [Ouala et al., 2019]



A person stands on a sandy beach with their arms raised in a gesture of triumph or achievement. The background is a vast ocean with waves breaking. Overlaid on the entire scene is a semi-transparent grid of binary code (0s and 1s) in a light blue color, creating a digital or technological atmosphere. The text is centered in the upper half of the image.

From proof-of-concept to actual impacts
what's needed /expected ?

From proof-of-concept to actual impacts: Panel session «JT IA-OAC, 06/02/2019»

Supporting the emergence of a scientific community Applied Math. - Data Science - OA Science

- Workshops, Data challenges, ... (e.g., AI4GeoDyn)
- Joint projects (e.g., LEFE-MANU IA-OAC, **ANR MeLODY**)

Computational resources and data management issues

- GPUs with data storage (e.g., Azure/Google, Jean Zay,...)
- Hosting reference datasets/data challenges

Supporting training initiatives

- Training course (e.g., Data Science for Geoscience)
- PhD/postdoc programs

Learning-based Downscaling for Ocean Currents [Fablet et al., 2019]

Currents

HR reference

HR prediction

LR input

Subgrid-scale
variance

Learnt differential
operators

$$\partial_s X = \phi(X) + \langle \nabla X, \psi(X) \rangle$$